White Paper

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Intel® Carry-Less Multiplication Instruction and its Usage for Computing the GCM Mode

The Intel® PCLMULQDQ instruction is a new instruction available beginning with the all new 2010 Intel® Core™ processor family based on the 32nm Intel® microarchitecture codename Westmere. The PCLMULQDQ instruction performs carry-less multiplication of two 64-bit operands.

This paper provides information on the instruction, and its usage for computing the Galois Hash. It also provides code examples for the usage of PCLMULQDQ, together with the Intel® AES New Instructions for efficient implementation of AES in Galois Counter Mode (AES-GCM).

This version of the paper also provides high performance code examples for AES-GCM, and discloses, for the first time, their measured performance numbers.

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Introduction

PCLMULQDQ is a new processor instruction that Intel is introducing in the 2010 Intel® Core™ processor family based on the 32nm Intel® microarchitecture codename Westmere, entering production starting the end of 2009. It computes the carry-less product of two 64-bit operands.

This paper provides details the PCLMULQDQ instruction, and describes several algorithms for using it for computing the Galois Hash, which is the underlying computation of the Galois Counter Mode (GCM).

An important usage model is AES in Galois counter Mode (AES-GCM), where the AES encryption/decryption part can be implemented efficiently using the Intel AES New Instructions which are also being introduced (see Reference [17], http://software.intel.com/en-us/articles/advanced-encryption-standard-aes-instructions-set/ for details) . This paper provides code examples for AES-GCM, using the new instructions, and also discloses their resulting performance.

This version of the paper provides high performance code examples for AES-GCM, and discloses, for the first time, their measured performance numbers.

Preliminaries

Usage Models of Carry-less Multiplication

Carry-less multiplication is the mathematical operation of computing the (carry-less) product of two operands without the generation or propagation of carry values. It is a relatively time consuming operation when implemented with the current ISA of the IA architecture. For example, software implementation of carry-less multiplication that uses one of the best-known methods (found at the OpenSSL source code distribution, www.openssl.org) computes a 64 by 64 bit carry-less product in about 100 cycles.

Carry-less multiplication is an essential processing component of several cryptographic systems and standards. Hence, accelerating carry-less multiplication can significantly contribute to achieving high speed secure computing and communication. Carry-less multiplication is especially important for implementing the Galois Counter Mode (GCM), which is a recently defined mode of operation of block ciphers [4, 6, 7, 8, 14, 15]. The GCM mode was endorsed by the US government in April 2006 and is used together with AES, which is part of the NSA Suite B. It is also defined in IEEE 802.1ae standard, where it is recommended for forwarding rates higher than 10 Gbps. Other usage models of GCM include IPsec (IPsec RFC 4106), the storage standard P1619 and security protocols over fiber channel (ISO-T11 standard).

GCM performs carry-less multiplication of 128-bit operands, producing a 255-bit product. This is the first step of computing a 'Galois hash', which is part of the GCM mode. The PCLMULQDQ instruction computes the 127-bit product of two 64-bit operands. It can be used by software as a building block for generating the 255-bit result required for GCM.

The other step in GCM is reduction modulo of a pentanomial $x^{128} + x^7 + x^2 + x + 1$. In this document, we describe a new efficient algorithm for performing this reduction in the Intel® SSE domain (using PSRLD, PSLLD PSHUFD instructions). The combination of the PCLMULQDQ instruction, together with this algorithm speeds up the GCM mode.

Carry-less multiplication is also in the core computation of Elliptic Curve Cryptography (ECC) over binary fields [2] and Cyclic Redundancy Checks (CRCs). The carry-less multiplication instruction PCLMULQDQ can speedup the computation of CRC with polynomials other than the iSCSI polynomial, for which there is already a dedicated instruction in the ISA (namely, CRC32 that is part of the Intel SSE4 set).

Carry-Less Multiplication - Definition

Carry-less multiplication is the operation of multiplying two operands without generating and propagating carries. It is formally defined as follows. Let the two operands *A*, *B*, be defined by the following n-bit array notation

$$A = [a_{n-1}\ a_{n-2}\ \ldots\ a_0],\ \ B = [b_{n-1}\ b_{n-2}\ \ldots\ b_0] \qquad (1)$$

and let the carry-less multiplication result be the following 2n-1 bit array:

$$C = [c_{2n-2}\ c_{2n-2}\ \ldots\ c_0] \qquad (2)$$

The bits of the output *C* are defined as the following logic functions of the bits of the inputs *A* and *B* as follows:

$$c_i = \bigoplus_{j=0}^{i} a_j b_{i-j} \qquad (3)$$

for $0 \le i \le n-1$, and

$$c_i = \bigoplus_{j=i-n+1}^{n-1} a_j b_{i-j} \qquad (4)$$

for $n \le i \le 2n-2$.

One can see that the logic functions of Equations (3) and (4) are somehow analogous to integer multiplication in the following sense. In integer multiplication, the first operand is shifted as many times as the positions of bits equal to "1" in the second operand. The integer multiplication is obtained by adding the shifted versions of the first operand with each other. The same procedure is followed in carry-less multiplication, but the "additions" do not generate or propagate carry, and are equivalent to the exclusive OR (XOR) logical operation.

Hereafter, carry-less multiplication is denoted by the symbol "•".

Carry-less Multiplication and Galois Field Multiplication

Typically, carry-less multiplication is used as the first step of multiplications in finite fields (aka Galois Fields) of characteristic 2 [10, 11, 12, 13].

A Galois Field is a finite set of elements where the operations addition '+' and multiplication '·' are defined. The set is closed under these operations where they satisfy the following properties: associativity, commutativity, existence of a neutral element (for addition it is called "0" and for multiplication it is called "1"), existence of additive inverse, existence of multiplicative inverse for each element except for zero, and a distributive law for multiplication over addition (i.e., a·(b+c) = a·b+a·c).

The number of elements of a finite field must be a power of some prime *p*, where in such case the field is denoted by GF(p^k). A binary field (field with characteristic 2) is the case where *p*=2, and is denoted by GF (2^k).

In general, the elements in GF(p^k) can be viewed as polynomials of degree *k* where the operations are defined using some irreducible polynomial of degree *k*: addition of two elements is defined as polynomial addition (adding the corresponding coefficients modulo *p*). Multiplication is defined by polynomial multiplication, which is subsequently reduced modulo the irreducible polynomial that defines the finite field.

Typically, there are multiple different irreducible polynomials of degree *k*. Using them to define the finite field results in isomorphic representations of the field.

For binary fields GF (2^n), one can view the elements as n-bit strings, where each bit represents the corresponding coefficient of the polynomial. In such cases, addition is equivalent to the bitwise XOR of the two strings. Multiplication consists of two steps. The first step is carry-less multiplication of the two operands. The second step is the reduction of this carry-less product modulo the polynomial that defines that field.

For example, consider the field GF(2^4) (i.e., n=4) defined by the reduction polynomial x^4+x+1. Let A = [1110] and B = [1011] be two elements in that field. Then, their product in this field is [1000]. This result is obtained as follows: Performing the carry-less multiplication C = A • B results in [01100010]. This is followed by reducing C modulo x^4+x+1. The reduction result is obtained by finding that [01100010] = [0110] • [10011] XOR [1000].

PCLMULQDQ Instruction Definition

PCLMULQDQ instruction performs carry-less multiplication of two 64-bit quadwords which are selected from the first and the second operands according to the immediate byte value.

Instruction format: PCLMULQDQ xmm1, xmm2/m128, imm8
Description: Carry-less multiplication of one quadword (8 bytes) of xmm1 by one quadword (8 bytes) of xmm2/m128, returning a double quadword (16 bytes). The immediate byte is used for determining which quadwords of

xmm1 and xmm2/m128 should be used. **Opcode:** 66 0f 3a 44 The presence of PCLMULQDQ is indicated by the CPUID leaf 1 ECX[1]. Operating systems that support the handling of Intel SSE state will also support applications that use AES extensions and the PCLMULQDQ instruction. This is the same requirement for Intel SSE2, Intel SSE3, Intel SSSE3, and Intel SSE4.

The immediate byte values are used as follows.

imm[7:0]	Operation
0x00	xmm2/m128[63:0] • xmm1[63:0]
0x01	xmm2/m128[63:0] • xmm1[127:64]
0x10	xmm2/m128[127:64] • xmm1[63:0]
0x11	xmm2/m128[127:64] • xmm1[127:64]

NOTE:

1. The symbol "•" denotes carry-less multiplication
2. Immediate bits other than 0 and 4 are ignored.

The pseudo code for defining the operation is as follows.

```
IF imm8[0] == 0 THEN
        Temp1 = xmm1[63:0]
ELSE
        Temp1 = xmm1[127:64]
ENDIF
IF imm8[4] == 0 THEN
        Temp2 = xmm2/m128[63:0]
ELSE
        Temp2 = xmm2/m128[127:64]
ENDIF
FOR i = 0 TO  63
        TempB [i] := (Temp1[0] AND Temp2[i]);
        FOR j = 1 TO i, 1
                TempB [i] := TempB [i] XOR (Temp1[j] AND Temp2[i -j])
        NEXT j
        Dest[i] := TempB[i];
NEXT i
FOR i = 64 TO 126, 1
        TempB [i] := (Temp1[ i-63] AND Temp2[63]);
        FOR j = i-62 TO 63, 1
```

```
            TempB [i] := TempB [i] XOR (Temp1[j] AND Temp2[i -j])
        NEXT j
        Dest[i] := TempB [i];
    NEXT i
    Dest[127] := 0;
```

The AVX (Nondestructive Destination) Variant VPCLMULQDQ

The carry-less multiplication instruction PCLMULQDQ has a nondestrructive version (VEX.128 encoded version), namely, VPCLMULQDQ, which is defined as follows.

Instruction format: VPCLMULQDQ xmm1, xmm2, xmm3/m128, imm8

Description: Carry-less multiplication of one quadword of xmm2 by one quadword of xmm3/m128, returning a double quadword (16 bytes) in register xmm1. The immediate is used for determining which quadwords of xmm2 and xmm3/m128 should be carry-less multiplied. The immediate byte is used exactly as in PCLMULQDQ. Functionally, this provides a non-destructive variant of PCLMULQDQ.

Opcode: VEX.NDS.128.66.0F3A 44 /r ib

The presence of VPCLMULQDQ is indicated by CPUID leaf 1 ECX[1].

The instruction operates on xmm states. The detection sequence must combine checking for CPUID.01H:ECX.PCLMULQDQ[bit 1] = 1, and the sequence for detection application support for GSSE.

Bits (255:128) of the destination ymm register are zeroed.

Identifying PCLMULQDQ Support by the Processor

Before an application attempts to use the PCLMULQDQ instruction it should check for its availability, which is indicated if CPUID.01H:ECX.PCLMULQDQ[bit 1] = 1.

Operating systems that support handling Intel® SSE state support also applications that use PCLMULQDQ. This is the same requirement for Intel SSE2, Intel SSE3, Intel SSSE3, and Intel SSE4.

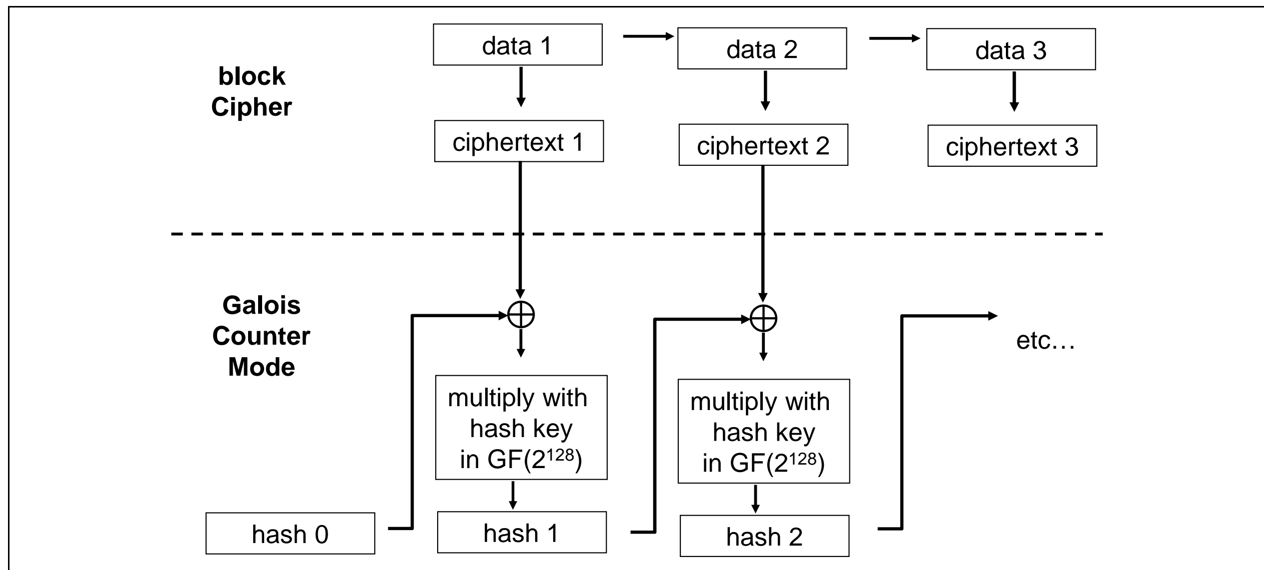
The Galois Counter Mode (GCM)

This section described the Galois Counter Mode and its current lookup table based software implementation (see for example [5] and www.openssl.org).

The Definition of GCM

The Galois Counter Mode is illustrated in Figure 1. This mode produces a message digest, called "Galois Hash'", from the encrypted data. This Galois Hash is used for high performance message authentication. In each step of the mode, the previous Galois Hash value is XOR-ed with the current ciphertext block. The result is then multiplied in GF(2^{128}) with a hash key value. GCM uses GF(2^{128}) defined by the irreducible polynomial $g = g(x) = x^{128} + x^7 + x^2 + x + 1$.

Figure 1. The Galois Counter Mode



The multiplication in GF(2^{128}) involves carry-less multiplication of two 128-bit operands, to generate a 255-bit result (or, equivalently, 256-bit result, where the most significant bit equals 0), followed by and reduction modulo the irreducible polynomial *g*.

Current Software Implementation of GCM

Some of the current software implementations of GCM implement the Galois Filed multiplication directly. Such implementations are not very efficient when using only the current IA instructions set. One example is given in Figure 2, taken from OpenSolaris. Solaris has C function gcm_mul() that takes two 64-bit elements (*x_in and *y in Figure 2), and places their carryless product in a third 64-bit integer (*res). Figure 2 is the current C source code from http://src.opensolaris.org/source/xref/onnv/onnv-gate/usr/src/common/crypto/modes/gcm.c#46 (Copyright 2009 Sun Microsystems, Inc.)

Figure 2. The OpenSolaris "gfmul" C Function

```
/* copied from
http://src.opensolaris.org/source/xref/onnv/onnv-
gate/usr/src/common/crypto/modes/gcm.c#46
(Copyright 2009 Sun Microsystems, Inc.)
 */
#include <stdint.h>
#include <wmmintrin.h>
struct aes_block {
    uint64_t a;
    uint64_t b;
};
void
gfmul(__m128i x_in_m, __m128i y_m, uint64_t *res)
{
    uint64_t R = { 0xe100000000000000ULL };
    struct aes_block z = { 0, 0 };
    struct aes_block v;
    uint64_t x;
    int i, j;
    uint64_t *x_in=(uint64_t*)&x_in_m;
    uint64_t *y=(uint64_t*)&y_m;

    v.a=y[1];
    v.b=y[0];

    for (j = 1; j>=0; j--) {
        x = x_in[j];
        for (i = 0; i < 64; i++, x <<= 1) {
            if (x & 0x8000000000000000ULL) {
                z.a ^= v.a;
                z.b ^= v.b;
            }
            if (v.b & 1ULL) {
                v.b = (v.a << 63)|(v.b >> 1);
                v.a = (v.a >> 1) ^ R;
            } else {
                v.b = (v.a << 63)|(v.b >> 1);
                v.a = v.a >> 1;
            }
        }
    }
    res[0] = z.b;
    res[1] = z.a;
}
```

A more optimized software implementations of the GCM mode use a lookup table based algorithm [5], shown in Figure 3 (for AES-GCM). The pseudo-code of Figure 3 does not take into account bit and byte reflection peculiarities of GCM implementations. This algorithm consists of two phases:

Preprocessing phase: generation of 16 lookup tables. Each table has 256 128-bit entries where entry j of table T_i stores the value (j * *hash key* * 2^{8i}) mod g for j =0, 1, …255, and i = 0, 1, …, 15

Run time phase: The algorithm takes the next ciphertext block and XOR-s it with the current value of the Galois Hash. The result (dynamic value) is multiplied with the Hash Key (fixed value) in GF(2^{128}). The GF(2^{128}) multiplication is carried out as follows: the value of the result is segmented into 16 8-bit slices. Subsequently, 16 table lookups are performed, using the slices, for indexing the tables. The results from the table lookups are XOR-ed with each other.

This algorithm performs operations on a per-byte basis: each 128-bit block involves 16 table lookups and 16 128-bit XOR operations.

This algorithm is not very efficient in software due to the cost of table lookups. It also suffers from potential side channel leakage based on memory access patterns (the accessed cache lines for the table lookup are data dependent).

Figure 3. Lookup Table Based Implementation of AES-GCM

```
// Code snippet illustrating AES-GCM (AES-128)
// The AES round keys are assumed to be already expanded
//
           m128i enc_data[length];
          _m128i IV;
          _m128i counter;
          _m128i roundkeys[11];
          _m128i temp;
          _m128i galoishash;
          _m128i tables[16][256]
int i;
initall();
init_galoishash();
copy128(counter, IV);
for(i=0; i < length; i++)
   {
    copy128(temp, counter);
    xor128(temp, roundkeys[0]);
    for(j=0; j <9; j++)
            aes_encrypt_round(temp, roundkeys[j+1]);
    aes_encrypt_last_round(temp, roundkeys[10]);
    xor128(temp, data[i]);
    copy128(enc_data[i], temp);
    add128(counter, 1);
    xor128(galoishash, enc_data);
    uint8_t *bytes_gh = (uint8_t *)galoishash;
    copy128(temp, 0);
    for(j=0; j < 16; j++)
        xor128(temp, tables[j][bytes_gh[j]]);
       // tables[i][j] = j*hash_key*256*i mod x^128 + x^7 + x^2 + x + 1
    copy128(galoishash, temp);
    }
```

Efficient Algorithms for Computing GCM

This section describes several new methods for computing the Galois Counter Mode. This method is an extension of the algorithm described in [6, 7].

The method described here uses the 64-bit PCLMULQDQ instruction in place of the lookup table method, for computing 128-bit-by-128-bit carry-less products, and an efficient novel method for reducing the result modulo the irreducible polynomial g of the finite field GF(2^{128}). The proposed algorithms are carried out in two steps: carry-less multiplication and reduction modulo $g = x^{128} + x^7 + x^2 + x + 1$.

Performing Carry-less Multiplication of 128-bit Operands Using PCLMULQDQ

Denote the input operands by $[A_1:A_0]$ and $[B_1:B_0]$, where A_0, A_1, B_0 and B_1 are 64 bit long each.

The following algorithm can be viewed as "one iteration carry-less schoolbook'" multiplication.

Algorithm 1

Step 1: multiply carry-less the following operands: A_0 with B_0, A_1 with B_1, A_0 with B_1, and A_1 with B_0. Let the results of the above four multiplications be:

$$A_0 \bullet B_0 = [C_1 : C_0],\ \ A_1 \bullet B_1 = [D_1 : D_0],\ \ A_0 \bullet B_1 = [E_1 : E_0],\ \ A_1 \bullet B_0 = [F_1 : F_0]$$

Step 2: construct the 256-bit output of the multiplication $[A_1:A_0] \bullet [B_1:B_0]$ as follows:

$$[A_1 : A_0] \bullet [B_1 : B_0] = [D_1 : F_1 \oplus E_1 \oplus D_0 : F_0 \oplus E_0 \oplus C_1 : C_0] \qquad (5)$$

An alternative technique trades-off one multiplication for additional XOR operations. It can be viewed as "one iteration carry-less Karatsuba" multiplication [7, 9].

Algorithm 2

Step 1: multiply carry-less the following operands: A_1 with B_1, A_0 with B_0, and $A_0 \oplus A_1$ with $B_0 \oplus B_1$. Let the results of the above three multiplications be: $[C_1:C_0]$, $[D_1:D_0]$ and $[E_1:E_0]$, respectively.

Step 2: construct the 256-bit output of the multiplication $[A_1:A_0]$ * $[B_1:B_0]$ as follows:

$$[A_1 : A_0] \bullet [B_1 : B_0] = [C_1 :\ C_0 \oplus C_1 \oplus D_1 \oplus E_1 : D_1 \oplus C_0 \oplus D_0 \oplus E_0 : D_0] \qquad (6)$$

Efficient Reduction Algorithm

To reduce a 256-bit carry-less product modulo a polynomial g of degree 128, we first split it into two 128-bit halves. The least significant half is simply XOR-ed with the final remainder (since the degree of g is 128).

For the most significant part, we develop an algorithm that realizes division via two multiplications. This algorithm can be seen as an extension of the Barrett reduction algorithm [1] to modulo-2 arithmetic, or as an extension of the Feldmeier CRC generation algorithm [3] to dividends and divisors of arbitrary size.

Since we do not need to take into account the least significant half of the input (see above), we investigate the efficient generation of a remainder $p(x)$ defined as follows:

$$p(x) = c(x) \cdot x^t \bmod g(x) \quad (7)$$

Where,

1. $c(x)$ is a polynomial of degree s-1 with coefficients in GF(2), representing the most significant bits of the carry-less product. (for GCM, s =128).
2. t is the degree of the polynomial g. (for GCM, t= 128).
3. $g(x)$ is the irreducible polynomial defining the final field (for GCM, g = $g(x) = x^{128} + x^7 + x^2 + x + 1$).

For the polynomials $p(x)$, $c(x)$, and $g(x)$ we write:

$$c(x) = c_{s-1}x^{s-1} + c_{s-2}x^{s-2} + \ldots + c_1 x + c_0 ,$$

$$p(x) = p_{t-1}x^{t-1} + p_{t-2}x^{t-2} + \ldots + p_1 x + p_0 \text{, and} \quad (8)$$

$$g(x) = g_t x^t + g_{t-1}x^{t-1} + \ldots + g_1 x + g_0$$

Hereafter, we use the notation $L^u(v)$ to denote the coefficients of the u least significant terms of the polynomial v and $M^u(v)$ to denote the coefficients of its u most significant terms. The polynomial $p(x)$ can be expressed as:

$$p(x) = c(x) \cdot x^t \bmod g(x) = g(x) \cdot q(x) \bmod x^t \quad (9)$$

where $q(x)$ is a polynomial of degree s-1 equal to the quotient from the division of $c(x) \cdot x^t$ with g. The intuition behind equation (9) is that the t least significant terms of the dividend $c(x) \cdot x^t$ equal zero. Further, the dividend $c(x) \cdot x^t$ can be expressed as the sum of the polynomials $g \cdot q$ and p:

$$c(x) \cdot x^t = g(x) \cdot q(x) + p(x) \quad (10)$$

where operator '+' means XOR ('⊕'). From equation (10) one can expect that the t least significant terms of the polynomial $g \cdot q$ are equal to the terms of the polynomial p. Only if these terms are equal to each other, the result of the XOR operation $g \cdot q \oplus p$ is zero for its t least significant terms. Hence:

$$p(x) = g(x) \cdot q(x) \bmod x^t = L^t(g(x) \cdot q(x)) \quad (11)$$

Now we define

$$g(x) = g_t x^t + g^*(x) \quad (12)$$

The polynomial g^* represents the t least significant terms of the polynomial g. Obviously,

$$p(x) = L^t(g(x) \cdot q(x)) = L^t(q(x) \cdot g^*(x) + q(x) \cdot g_t x^t) \tag{13}$$

However, the t least significant terms of the polynomial $q \cdot g_t \cdot x^t$ are zero. Therefore,

$$p(x) = L^t(q(x) \cdot g^*(x)) \tag{14}$$

From Equation (14) it follows that in order to compute the remainder p we need to know the value of the quotient q. The quotient can be calculated in a similar manner as in the Barrett reduction algorithm:

$$(9) \Leftrightarrow c(x) \cdot x^{t+s} = g(x) \cdot q(x) \cdot x^s + p(x) \cdot x^s \tag{15}$$

Let

$$x^{t+s} = g(x) \cdot q^+(x) + p^+(x) \tag{16}$$

where q^+ is an s-degree polynomial equal to the quotient from the division of x^{t+s} with g and p^+ is the remainder from this division. The degree of the polynomial p^+ is t-1. From equations (15) and (16) we get

$$\left.\begin{matrix}(15)\\(16)\end{matrix}\right\} \Leftrightarrow c(x) \cdot g(x) \cdot q^+(x) + c(x) \cdot p^+(x) \\ = g(x) \cdot q(x) \cdot x^s + p(x) \cdot x^s \tag{17}$$

and

$$(17) \Rightarrow M^s(c(x) \cdot g(x) \cdot q^+(x) + c(x) \cdot p^+(x)) \\ = M^s(g(x) \cdot q(x) \cdot x^s + p(x) \cdot x^s) \tag{18}$$

One can see that the polynomials $c \cdot g \cdot q^+$ and $g \cdot q \cdot x^s$ are of degree t+2·s-1 the polynomial $c \cdot p^+$ is of degree t+s-2, and the polynomial $p \cdot x^s$ is of degree t+s-1. As a result the s most significant terms of the polynomials in the left and right hand side of equation (18) are not affected by the polynomials $c \cdot p^+$ and $p \cdot x^s$. Hence,

$$(18) \Leftrightarrow M^s(c(x) \cdot g(x) \cdot q^+(x)) \\ = M^s(g(x) \cdot q(x) \cdot x^s) \tag{19}$$

Next, we observe that the s most significant terms of the polynomial $c \cdot g \cdot q^+$ equal to the s most significant terms of the polynomial $g \cdot M^s(c \cdot q^+) \cdot x^s$. The polynomial $M^s(c \cdot q^+) \cdot x^s$ results from $c \cdot q^+$ by replacing the s least significant terms of this polynomial with zeros. The intuition behind this observation is the following: the s most significant terms of the polynomial $c \cdot g \cdot q^+$ are calculated by adding the s most significant terms of the polynomial $c \cdot q^+$ with each other in as many offset positions as defined by the terms of

the polynomial g. Thus, the s most significant terms of $c{\cdot}g{\cdot}q^+$ do not depend on the s least significant terms of $c{\cdot}q^+$, and consequently,

$$\begin{aligned}(19) &\Leftrightarrow M^s(g(x)\cdot M^s(c(x)\cdot q^+(x))\cdot x^s)\\ &= M^s(g(x)\cdot q(x)\cdot x^s)\end{aligned} \tag{20}$$

Equation (20) is satisfied for q given by

$$q = M^s(c(x)\cdot q^+(x)) \tag{21}$$

Since there is a unique quotient q satisfying equation (10) one can show that there is a unique quotient q satisfying equation (20). As a result this quotient q must be equal to $M^s(c(x){\cdot}q^+(x))$.

It follows that the polynomial p is found by

$$p(x) = L^t(g^*(x)\cdot M^s(c(x)\cdot q^+(x))) \tag{22}$$

Equation (22) indicates the algorithm for computing the polynomial p.

Algorithm 3:

Preprocessing: For the given irreducible polynomial g the polynomials g^* and q^+ are computed first. The polynomial g^* is of degree t-1 consisting of the t least significant terms of g, whereas the polynomial q^+ is of degree s and is equal to the quotient of the division of x^{t+s} with the polynomial g.

Calculation of the remainder polynomial:

Step 1: The input c is multiplied with q^+. The result is a polynomial of degree 2s-1.

Step 2: The s most significant terms of the polynomial resulting from step 1 are multiplied with g^*. The result is a polynomial of degree t+s-2.

Step 3: The algorithm returns the t least significant terms of the polynomial resulting from step 2. This is the desired remainder.

Application of the method for reduction modulo $x^{128} + x^7 + x^2 + x + 1$

One can see that the quotient from the division of x^{256} with g is g itself. The polynomial g = $g(x) = x^{128} + x^7 + x^2 + x + 1$ contains only 5 non-zero coefficients (therefore also called "pentanomial"). This polynomial can be represented as the bit sequence [1:<*120 zeros*>:10000111]. Multiplying this carry-less with a 128-bit value and keeping the 128 most significant bit can be obtained by: (i) Shifting the 64 most significant bits of the input by 63, 62 and 57-bit positions to the right. (ii) XOR-ing these shifted copies with the 64 least significant bits of the input. Next, we carry-less multiply this 128-bit result with g, and keep the 128 least significant bits. This can be done by: (i) shifting the 128-bit input by 1, 2 and 7 positions to the left. (ii) XOR-ing the results. Algorithm 4 provides a detailed description of the reduction algorithm.

Algorithm 4

Denote the input operand by $[X_3:X_2:X_1:X_0]$ where X_3, X_2, X_1 and X_0 are 64 bit long each.

Step 1: shift X_3 by 63, 62 and 57-bit positions to the right. Compute the following numbers:

$$\begin{aligned} A &= X_3 >> 63 \\ B &= X_3 >> 62 \\ C &= X_3 >> 57 \end{aligned} \quad (23)$$

Step 2: We XOR A, B, and C with X_2. We compute a number D as follows:

$$D = X_2 \oplus A \oplus B \oplus C \quad (24)$$

Step 3: shift $[X_3:D]$ by 1, 2 and 7 bit positions to the left. Compute the following numbers:

$$\begin{aligned} [E_1 : E_0] &= [X_3 : D] << 1 \\ [F_1 : F_0] &= [X_3 : D] << 2 \\ [G_1 : G_0] &= [X_3 : D] << 7 \end{aligned} \quad (25)$$

Step 4: XOR $[E_1:E_0]$, $[F_1:F_0]$, and $[G_1:G_0]$ with each other and $[X_3:D]$. Compute a number $[H_1:H_0]$ as follows:

$$[H_1 : H_0] = [X_3 \oplus E_1 \oplus F_1 \oplus G_1 : D \oplus E_0 \oplus F_0 \oplus G_0] \quad (26)$$

Return $[X_1 \oplus H_1 : X_0 \oplus H_0]$.

Bit Reflection Peculiarity of GCM

Special peculiarity should be taken into account when implementing the GCM mode, because the standard specifies that the bits inside their 128-bit double-quad-words are reflected.

Definition: For a 128 bits quantity Q, Reflect (Q) is defined as the 128 bits quantity R whose i-th bit equal to the (127-i)-th bit of R, (for 0 ≤ i ≤ 127).

This peculiarity applies to the two operands being multiplied in the finite field GF(2^{128}) (defined by the specification), and also to the order of bits in the reduction polynomial, which is [11100001:<*120 zeros*>:1] as opposed to [1:<*120 zeros*>:10000111].

Note that this peculiarity is not merely the difference between Little Endian and Big Endian notations.

We discuss here two approaches for handling the bit reflection peculiarity.

Bit Reflecting the Inputs

One approach for way handle the bit reflection peculiarity is to bit-reflect the input to the gfmul function. In GCM, one of the inputs is fixed for the whole process (it is the

hash key), it can be reflected once generated. The other inputs need to be reflected as they are produced (by the AES-CTR module).

A simple way to implement bit reflection is to use lookup tables. Ideally we want to use an 8bit → 8bit lookup table, that matches a byte to its reflected value, and then swap the order of the bytes, as required. However, a more efficient way is to implement bit reflection using a 4bit → 4bit lookup table, which can fit into a single xmm register, and to apply the PSHUFB instruction in some sophisticated way.

To bit reflect a 128bit quantity (in an xmm), we first isolate the 4bit nibbles within each byte. Then we can reflect the nibble (8 at a time) by using PSHUFB with some pre-computed (constant) masks stored in two other xmm registers. We illustrate the method with the following example.

This is the contents of xmm1:

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0x56	0xff	0x13	0x00	0x09	0x43	0xb2	0x4a	0x17	0x8d	0xfc	0x3a	0xfd	0x34	0x43	0x11

xmm1 is copied to xmm2 and the nibbles are isolated in each xmm:

xmm1 holds the lower nibbles (in each byte):

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0x06	0x0f	0x03	0x00	0x09	0x03	0x02	0x0a	0x07	0x0d	0x0c	0x0a	0x0d	0x04	0x03	0x01

xmm2 holds the upper nibbles (in each byte):

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0x05	0x0f	0x01	0x00	0x00	0x04	0x0b	0x04	0x01	0x08	0x0f	0x03	0x0f	0x03	0x04	0x01

Now let xmm3 and xmm4 hold the reflected values of the 16 possible nibbles

xmm3 holds the low reflected nibbles:

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0x0f	0x07	0x0b	0x03	0x0d	0x05	0x09	0x01	0x0e	0x06	0x0a	0x02	0x0c	0x04	0x08	0x00

xmm4 holds the high reflected nibbles:

15	14	13	12	11	10	9	8	7	6	5	4	3	2	1	0
0xf0	0x70	0xb0	0x30	0xd0	0x50	0x90	0x10	0xe0	0x60	0xa0	0x20	0xc0	0x40	0x80	0x00

Now by using xmm1 and xmm2 as the mask and xmm3 with xmm4 as the operand, one will have the reflected nibbles in the right order in xmm3 and xmm4. By adding them and using another PSHUFB to swap the order of bytes, the reflected value of the whole xmm is obtained.

This method can be used to implement any 4bit → 4bit lookup table.

Figure 4. Code Sample – Reflecting Bits of a 128-bits Quantity

```
#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>

__m128i reflect_xmm(__m128i X)
{
    __m128i tmp1,tmp2;

    __m128i AND_MASK =
        _mm_set_epi32(0x0f0f0f0f, 0x0f0f0f0f, 0x0f0f0f0f, 0x0f0f0f0f);
    __m128i LOWER_MASK =
        _mm_set_epi32(0x0f070b03, 0x0d050901, 0x0e060a02, 0x0c040800);
    __m128i HIGHER_MASK =
        _mm_set_epi32(0xf070b030, 0xd0509010, 0xe060a020, 0xc0408000);
    __m128i BSWAP_MASK =
        _mm_set_epi8(0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15);

    tmp2 = _mm_srli_epi16(X, 4);
    tmp1 = _mm_and_si128(X, AND_MASK);
    tmp2 = _mm_and_si128(tmp2, AND_MASK);
    tmp1 = _mm_shuffle_epi8(HIGHER_MASK ,tmp1);
    tmp2 = _mm_shuffle_epi8(LOWER_MASK ,tmp2);
    tmp1 = _mm_xor_si128(tmp1, tmp2);
    return _mm_shuffle_epi8(tmp1, BSWAP_MASK);
}
```

Avoiding Bit Reflecting

Here, we show an alternative that helps avoiding bit reflecting the inputs. We start with the following fundamental property of carry-less multiplication:

$$reflected\ (A) \bullet reflected\ (B) = reflected\ (A \bullet B) >> 1 \tag{27}$$

Using this identity, the PCLMULQDQ instruction can be used for performing multiplication in the finite field GF(2^{128}) seamlessly, regardless on the representation of the input and the output operands.

Algorithm 5 outlines the required modification of the reduction algorithm that accommodates bit reflection of the inputs and the outputs in the GCM mode.

Algorithm 5

Denote the input operand by $[X_3:X_2:X_1:X_0]$ where X_3, X_2, X_1 and X_0 are 64 bit long each.

Step 1: compute

$$[X_3 X_2 X_1 X_0] = [X_3 X_2 X_1 X_0] << 1 \tag{28}$$

Step 2: shift X_0 by 63, 62 and 57 bit positions to the left. We compute the following numbers:

$$A = X_0 << 63$$
$$B = X_0 << 62 \quad (29)$$
$$C = X_0 << 57$$

Step 2: XOR *A*, *B*, and *C* with X_1. Compute a number *D* as follows:

$$D = X_1 \oplus A \oplus B \oplus C \quad (30)$$

Step 3: shift $[D{:}X_0]$ by 1, 2 and 7 bit positions to the right. Compute the following numbers:

$$[E_1 : E_0] = [D : X_0] >> 1$$
$$[F_1 : F_0] = [D : X_0] >> 2 \quad (31)$$
$$[G_1 : G_0] = [D : X_0] >> 7$$

Step 4: XOR $[E_1{:}E_0]$, $[F_1{:}F_0]$, and $[G_1{:}G_0]$ with each other and $[D{:}X_0]$. Compute a number $[H_1{:}H_0]$ as follows:

$$[H_1 : H_0] = [D \oplus E_1 \oplus F_1 \oplus G_1 : X_0 \oplus E_0 \oplus F_0 \oplus G_0] \quad (32)$$

Return $[X_3 \oplus H_1{:}\ X_2 \oplus H_0]$.

The advantage of this method, over reflecting the inputs (as shows above) is that it does not require the data to be reflected. This allows for aggregating several reductions together, for a more efficient over all implementation, as shown below.

Implementation Using Linear Folding

Linear folding is the mathematical operation of replacing a number of most significant bits of a quantity with the product of these bits times a constant during a reduction. Folding helps with speeding up reduction because it decreases the length of the quantity which is being reduced at the expense of the number of multiplications needed. In what follows we assume that all operations that take place are carry-less, i.e., in GF(2) arithmetic.

Suppose that the quantity to be reduced can be expressed as the sum of two polynomials:

$$p(x) = (c(x) \cdot x^t + d(x)) \bmod \ g(x) \quad (33)$$

Where,

1. $c(x)$ is a polynomial of degree s-1 with coefficients in GF(2), representing the most significant bits of the quantity to be reduced
2. t-1 is the length of the degree of $d(x)$
3. $g(x)$ is the irreducible polynomial defining the field (for GCM, g = $g(x) = x^{128} + x^7 + x^2 + x + 1$).

For the polynomial $p(x)$ we write:

$$\begin{aligned} p(x) &= (c(x)\cdot x^t + d(x)) \bmod g(x) = \\ & c(x)\cdot x^t \bmod g(x) + d(x) \bmod g(x) = \\ & (c(x)\cdot (x^t \bmod g(x)) + d(x)) \bmod g(x) \end{aligned} \quad (34)$$

The quantity x^t mod $g(x)$ depends only on the reduction polynomial. Hence it can be treated as a constant. Equation (34) indicates a method for performing reduction which is called linear folding and works as follows:

Step 1: The polynomial $c(x)$ is multiplied carry-less with the constant x^t mod $g(x)$.

Step 2: The result of the multiplication is XOR-ed with $d(x)$.

Step 3: The reduction proceeds using any known technique.

The remainder from the division of x^t with $g(x) = x^{128} + x^7 + x^2 + x + 1$ is the bit sequence <10000111: t-128 zeros>. Since $t+s = 255$ one can see that the length of the carry-less multiplication of $c(x)$ with x^t mod $g(x)$ is 134 and is independent of the choice of t and s.

In GCM all operations are bit reflected, so folding needs to be implemented in a bit reflected manner too. The designer of an algorithm based on linear folding has several degrees of freedom that depend on the choice of t and s. If the length of the folding quantity $c(x)$ spans a single 64-bit word then the cost of multiplication with x^t mod $g(x)$ can be potentially small, equals to 1 or 2 64-bit carry-less multiplication operations. On the other hand the cost of further reducing the given polynomial after folding may be higher.

Another issue related to the design of a folding algorithm has to do with the fact that the reflected version of x^t mod $g(x)$ may span one or multiple words. Theoretically one can multiply $c(x)$ not with x^t mod $g(x)$ but with an appropriately shifted version of the bit sequence <11100001> so that the second operand of the multiplication spans exactly one 64 bit word. The result can then be corrected with further shift operations. There is one case for which the second operand of the multiplication spans one word and no further shifts are required: this is for $t = 193$. For this case, the subsequent reduction steps after folding requiring reducing a 193 bit quantity.

In what follows we describe four representative algorithms two for $s = 120$ and two for $s = 64$ bits. In each pair the second operand of the folding multiplication spans 1 or 2 words.

Algorithm 6: Folding length s = 120, two multiplications version

Denote the input operand by $[X_3:X_2:X_1:X_0]$ where X_3, X_2, X_1 and X_0 are 64 bit long each.

Step 1: Compute $[C_1:C_0]$ =$[X_1:X_0]$ AND 0x00ffffffffffffffffffffffffffff

Step 2: Compute $[H_2:H_1:H_0]$ =$[C_1:C_0]$ • 0xe100000000000000 (64 bit)

Step 3: Shift $[H_2:H_1:H_0]$ by one bit position to the left

Step 4: XOR $[H_2:H_1:H_0:0]$ with $[X_3:X_2:X_1:X_0]$ and replace $[X_3:X_2:X_1:X_0]$

Step 5: Replace X_1 with the result of logical AND between X_1 and 0xff00000000000000

Step 6: Compute A = X_1 &(1 << 63), B = X_1 << 1, C = (X_1 & 0x7f00000000000000) >> 1, D = (X_1 & 0x7f00000000000000) >> 6, E = X_1 & 0x7f00000000000000.

Step 7: Shift [X_3:X_2:A] by one bit position to the left

Return [$X_3 \oplus B \oplus C \oplus D \oplus E$:$X_2$].

Algorithm 7: Folding length s = 120, four multiplications version

Denote the input operand by [X_3:X_2:X_1:X_0] where X_3, X_2, X_1 and X_0 are 64 bit long each.

Step 1: Compute [C_1:C_0] =[X_1:X_0] AND 0x00ffffffffffffffffffffffffffffff

Step 2: Compute [H_2:H_1:H_0] =[C_1:C_0] • 0x1c200000000000000 (*)

Step 3: XOR [H_2:H_1:H_0:0] with [X_3:X_2:X_1:X_0] and replace [X_3:X_2:X_1:X_0]

Step 4: Replace X_1 with the result of logical AND between X_1 and 0xff00000000000000

Step 5: Compute A = X_1 & 1(<< 63), B = X_1 << 1, C = (X_1 & 0x7f00000000000000) >> 1, D = (X_1 & 0x7f00000000000000) >> 6, E = X_1 & 0x7f00000000000000.

Step 6: Shift [X_3:X_2:A] by one bit position to the left

Return [$X_3 \oplus B \oplus C \oplus D \oplus E$:$X_2$].

(*) **Note**: 0x1c200000000000000 is a 65-bits quantity, and therefore four multiplications are required for computing [C_1:C_0] • 0x1c200000000000000

Algorithm 8: Folding length s = 64, single multiplication version

Denote the input operand by [X_3:X_2:X_1:X_0] where X_3, X_2, X_1 and X_0 are 64 bit long each.

Step 1: Compute [H_1:H_0] =X_0 • 0xe100000000000000 (64 bit)

Step 2: Shift [H_1:H_0] by one bit position to the left

Step 3: XOR [0:H_1:H_0:0] with [X_3:X_2:X_1:0] and replace [X_3:X_2:X_1:0]

Step 4: Compute A = X_1 & (1 <<63), B = X_1 << 1, C_1 = (X_1 & 0x7fffffffffffffff) >> 1, C_0 = X_1<<63, D_1 = (X_1 & 0x7fffffffffffffff) >> 6, D_0 = X_1<<58, E = X_1 & 0x7fffffffffffffff,

Step 5: Shift [X_3:X_2:A] by one bit position to the left

Return [$X_3 \oplus B \oplus C_1 \oplus D_1 \oplus E$:$X_2 \oplus D_0 \oplus C_0$].

Algorithm 9: Folding length s = 64, two multiplications version

Denote the input operand by $[X_3:X_2:X_1:X_0]$ where X_3, X_2, X_1 and X_0 are 64 bit long each.

Step 1: Compute $[H_2:H_1:H_0] = X_0 \bullet$ 0x1c200000000000000 (65 bit)

Step 2: XOR $[H_2:H_1:H_0:0]$ with $[X_3:X_2:X_1:0]$ and replace $[X_3:X_2:X_1:0]$

Step 3: Compute $A = X_1$ & (1 << 63), $B = X_1$ << 1, $C_1 = (X_1$ & 0x7fffffffffffffff) >> 1, $C_0 = X_1$<<63, $D_1 = (X_1$ & 0x7fffffffffffffff) >> 6, $D_0 = X_1$<<58, $E = X_1$ & 0x7fffffffffffffff,

Step 4: Shift $[X_3:X_2:A]$ by one bit position to the left

Return $[X_3 \oplus B \oplus C_1 \oplus D_1 \oplus E : X_2 \oplus D_0 \oplus C_0]$.

Aggregated Reduction Method

This method was proposed by Krzysztof Jankowski, Pierre Laurent (see [17]). It is a way to delay the reduction step and apply the reducing to the aggregated result only once every few multiplications.

The standard Ghash formula is the following:

$$Yi = [(X_i + Y_{i-1}) \bullet H] \bmod P \qquad (P = x^{128} + x^7 + x^2 + x + 1)$$

Instead, one can apply the following recursion:

$$Yi = [(X_i + Y_{i-1}) \bullet H] \bmod P$$

$$= [(X_i \bullet H) + (Y_{i-1} \bullet H)] \bmod P$$

$$= [(X_i \bullet H) + (X_{i-1} + Y_{i-2}) \bullet H^2] \bmod P$$

$$= [(X_i \bullet H) + (X_{i-1} \bullet H^2) + (X_{i-2} + Y_{i-3}) \bullet H^3] \bmod P$$

$$= [(X_i \bullet H) + (X_{i-1} \bullet H^2) + (X_{i-2} \bullet H^3) + (X_{i-3} + Y_{i-4}) \bullet H^4] \bmod P$$

This can be further expanded to any depth. The only overhead in this computation is the need to calculate the powers of H mod P in advance, but the gain is that reduction is required only once in a few blocks. As can be appreciated now, the use of the identity (27) is advantageous because the data (from the AES-CTR) does not need to be manipulated, as would be the case if we choose the bit reflect method.

A good choice, which we adopt here, is to compute one reduction every 4 blocks.

Code Examples: Ghash Computation

Figures 5-8 are assembly and C code examples for implementing the Galois Field multiplication portion of GCM, using some combinations of the algorithms described in the section "Efficient Algorithms for Computing GCM".

These codes implement the "gfmul" function which is, in the subsequent chapter, integrated into the full AES-GCM code.

Figures 5-6 implement the same algorithms – one example in C and the other example in assembly (AT&T syntax). The assembly code example can be compiled from an assembly file, using the gcc compiler, with –maes and –msse4 flags.

The code in Figure 7 implements a different selection of algorithms.

The code in Figure 8 implements the Aggregated Reduction Method

Figure 5. Code Sample - Performing Ghash Using Algorithms 1 and 5 (C)

```
#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>

void gfmul (__m128i a, __m128i b, __m128i *res){
    __m128i tmp0, tmp1, tmp2, tmp3, tmp4, tmp5, tmp6, tmp7, tmp8, tmp9;

    tmp3 = _mm_clmulepi64_si128(a, b, 0x00);
    tmp4 = _mm_clmulepi64_si128(a, b, 0x10);
    tmp5 = _mm_clmulepi64_si128(a, b, 0x01);
    tmp6 = _mm_clmulepi64_si128(a, b, 0x11);

    tmp4 = _mm_xor_si128(tmp4, tmp5);
    tmp5 = _mm_slli_si128(tmp4, 8);
    tmp4 = _mm_srli_si128(tmp4, 8);
    tmp3 = _mm_xor_si128(tmp3, tmp5);
    tmp6 = _mm_xor_si128(tmp6, tmp4);

    tmp7 = _mm_srli_epi32(tmp3, 31);
    tmp8 = _mm_srli_epi32(tmp6, 31);
    tmp3 = _mm_slli_epi32(tmp3, 1);
    tmp6 = _mm_slli_epi32(tmp6, 1);

    tmp9 = _mm_srli_si128(tmp7, 12);
    tmp8 = _mm_slli_si128(tmp8, 4);
    tmp7 = _mm_slli_si128(tmp7, 4);
    tmp3 = _mm_or_si128(tmp3, tmp7);
    tmp6 = _mm_or_si128(tmp6, tmp8);
    tmp6 = _mm_or_si128(tmp6, tmp9);

    tmp7 = _mm_slli_epi32(tmp3, 31);
    tmp8 = _mm_slli_epi32(tmp3, 30);
    tmp9 = _mm_slli_epi32(tmp3, 25);

    tmp7 = _mm_xor_si128(tmp7, tmp8);
    tmp7 = _mm_xor_si128(tmp7, tmp9);
    tmp8 = _mm_srli_si128(tmp7, 4);
    tmp7 = _mm_slli_si128(tmp7, 12);
    tmp3 = _mm_xor_si128(tmp3, tmp7);

    tmp2 = _mm_srli_epi32(tmp3, 1);
    tmp4 = _mm_srli_epi32(tmp3, 2);
    tmp5 = _mm_srli_epi32(tmp3, 7);
    tmp2 = _mm_xor_si128(tmp2, tmp4);
    tmp2 = _mm_xor_si128(tmp2, tmp5);
    tmp2 = _mm_xor_si128(tmp2, tmp8);
    tmp3 = _mm_xor_si128(tmp3, tmp2);
```

```
    tmp6 = _mm_xor_si128(tmp6, tmp3);

    *res = tmp6;
}
```

Figure 6. Code Sample - Performing Ghash Using Algorithms 1 and 5 (Assembly)

```
.globl    gfmul
gfmul:
        #xmm0 holds operand a (128 bits)
        #xmm1 holds operand b (128 bits)
        #rdi  holds the pointer to output (128 bits)

 movdqa     %xmm0, %xmm3
 pclmulqdq  $0, %xmm1, %xmm3     # xmm3 holds a0*b0
 movdqa     %xmm0, %xmm4
 pclmulqdq  $16, %xmm1, %xmm4     #xmm4 holds a0*b1
 movdqa     %xmm0, %xmm5
 pclmulqdq  $1, %xmm1, %xmm5      # xmm5 holds a1*b0
 movdqa     %xmm0, %xmm6
 pclmulqdq  $17, %xmm1, %xmm6     # xmm6 holds a1*b1
 pxor       %xmm5, %xmm4          # xmm4 holds a0*b1 + a1*b0
 movdqa     %xmm4, %xmm5
 psrldq     $8, %xmm4
 pslldq     $8, %xmm5
 pxor       %xmm5, %xmm3
 pxor       %xmm4, %xmm6          # <xmm6:xmm3> holds the result of
 # the carry-less multiplication of xmm0 by xmm1

 # shift the result by one bit position to the left cope for the fact
 # that bits are reversed
 movdqa   %xmm3, %xmm7
 movdqa   %xmm6, %xmm8
 pslld    $1, %xmm3
 pslld    $1, %xmm6
 psrld    $31, %xmm7
 psrld    $31, %xmm8
 movdqa   %xmm7, %xmm9
 pslldq   $4, %xmm8
 pslldq   $4, %xmm7
 psrldq   $12, %xmm9
 por      %xmm7, %xmm3
 por      %xmm8, %xmm6
 por      %xmm9, %xmm6

 #first phase of the reduction
 movdqa   %xmm3, %xmm7
 movdqa   %xmm3, %xmm8
 movdqa   %xmm3, %xmm9
 pslld    $31, %xmm7            # packed right shifting << 31
 pslld    $30, %xmm8            # packed right shifting shift << 30
 pslld    $25, %xmm9            # packed right shifting shift << 25
 pxor     %xmm8, %xmm7          # xor the shifted versions
 pxor     %xmm9, %xmm7

 movdqa   %xmm7, %xmm8
 pslldq   $12, %xmm7
 psrldq   $4, %xmm8
 pxor     %xmm7, %xmm3          # first phase of the reduction complete
 movdqa   %xmm3,%xmm2           # second phase of the reduction
```

```
movdqa   %xmm3,%xmm4
movdqa   %xmm3,%xmm5
psrld    $1, %xmm2             # packed left shifting >> 1
psrld    $2, %xmm4             # packed left shifting >> 2
psrld    $7, %xmm5             # packed left shifting >> 7

pxor     %xmm4, %xmm2          # xor the shifted versions
pxor     %xmm5, %xmm2
pxor     %xmm8, %xmm2
pxor     %xmm2, %xmm3
pxor     %xmm3, %xmm6          # the result is in xmm6
movdqu   %xmm6, (%rdi)         # store the result
ret
```

Figure 7. Code Sample - Performing Ghash Using Algorithms 2 and 4 with Reflected Input and Output

```
#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>

void gfmul (__m128i a, __m128i b, __m128i *res){
    __m128i tmp0, tmp1, tmp2, tmp3, tmp4, tmp5, tmp6,
            tmp7, tmp8, tmp9, tmp10, tmp11, tmp12;
    __m128i XMMMASK = _mm_setr_epi32(0xffffffff, 0x0, 0x0, 0x0);

    tmp3 = _mm_clmulepi64_si128(a, b, 0x00);
    tmp6 = _mm_clmulepi64_si128(a, b, 0x11);

    tmp4 = _mm_shuffle_epi32(a,78);
    tmp5 = _mm_shuffle_epi32(b,78);
    tmp4 = _mm_xor_si128(tmp4, a);
    tmp5 = _mm_xor_si128(tmp5, b);

    tmp4 = _mm_clmulepi64_si128(tmp4, tmp5, 0x00);
    tmp4 = _mm_xor_si128(tmp4, tmp3);
    tmp4 = _mm_xor_si128(tmp4, tmp6);

    tmp5 = _mm_slli_si128(tmp4, 8);
    tmp4 = _mm_srli_si128(tmp4, 8);
    tmp3 = _mm_xor_si128(tmp3, tmp5);
    tmp6 = _mm_xor_si128(tmp6, tmp4);

    tmp7 = _mm_srli_epi32(tmp6, 31);
    tmp8 = _mm_srli_epi32(tmp6, 30);
    tmp9 = _mm_srli_epi32(tmp6, 25);

    tmp7 = _mm_xor_si128(tmp7, tmp8);
    tmp7 = _mm_xor_si128(tmp7, tmp9);

    tmp8 = _mm_shuffle_epi32(tmp7, 147);

    tmp7 = _mm_and_si128(XMMMASK, tmp8);
    tmp8 = _mm_andnot_si128(XMMMASK, tmp8);
    tmp3 = _mm_xor_si128(tmp3, tmp8);
    tmp6 = _mm_xor_si128(tmp6, tmp7);

    tmp10 = _mm_slli_epi32(tmp6, 1);
```

```
    tmp3 = _mm_xor_si128(tmp3, tmp10);
    tmp11 = _mm_slli_epi32(tmp6, 2);
    tmp3 = _mm_xor_si128(tmp3, tmp11);
    tmp12 = _mm_slli_epi32(tmp6, 7);
    tmp3 = _mm_xor_si128(tmp3, tmp12);

    *res = _mm_xor_si128(tmp3, tmp6);
 }
```

Figure 8. Code Sample - Performing Ghash Using an Aggregated Reduction Method

```
#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>

void reduce4 (__m128i H1, __m128i H2, __m128i H3, __m128i H4,
              __m128i X1, __m128i X2, __m128i X3, __m128i X4, __m128i *res)
    {
    /*algorithm by Krzysztof Jankowski,  Pierre Laurent  - Intel*/
    __m128i H1_X1_lo, H1_X1_hi,
            H2_X2_lo, H2_X2_hi,
            H3_X3_lo, H3_X3_hi,
            H4_X4_lo, H4_X4_hi,
            lo, hi;
    __m128i tmp0, tmp1, tmp2, tmp3;
    __m128i tmp4, tmp5, tmp6, tmp7;
    __m128i tmp8, tmp9;


    H1_X1_lo = _mm_clmulepi64_si128(H1, X1, 0x00);
    H2_X2_lo = _mm_clmulepi64_si128(H2, X2, 0x00);
    H3_X3_lo = _mm_clmulepi64_si128(H3, X3, 0x00);
    H4_X4_lo = _mm_clmulepi64_si128(H4, X4, 0x00);

    lo = _mm_xor_si128(H1_X1_lo, H2_X2_lo);
    lo = _mm_xor_si128(lo, H3_X3_lo);
    lo = _mm_xor_si128(lo, H4_X4_lo);

    H1_X1_hi = _mm_clmulepi64_si128(H1, X1, 0x11);
    H2_X2_hi = _mm_clmulepi64_si128(H2, X2, 0x11);
    H3_X3_hi = _mm_clmulepi64_si128(H3, X3, 0x11);
    H4_X4_hi = _mm_clmulepi64_si128(H4, X4, 0x11);

    hi = _mm_xor_si128(H1_X1_hi, H2_X2_hi);
    hi = _mm_xor_si128(hi, H3_X3_hi);
    hi = _mm_xor_si128(hi, H4_X4_hi);

    tmp0 = _mm_shuffle_epi32(H1, 78);
    tmp4 = _mm_shuffle_epi32(X1, 78);
    tmp0 = _mm_xor_si128(tmp0, H1);
    tmp4 = _mm_xor_si128(tmp4, X1);
    tmp1 = _mm_shuffle_epi32(H2, 78);
    tmp5 = _mm_shuffle_epi32(X2, 78);
    tmp1 = _mm_xor_si128(tmp1, H2);
    tmp5 = _mm_xor_si128(tmp5, X2);
    tmp2 = _mm_shuffle_epi32(H3, 78);
```

```
    tmp6 = _mm_shuffle_epi32(X3, 78);
    tmp2 = _mm_xor_si128(tmp2, H3);
    tmp6 = _mm_xor_si128(tmp6, X3);
    tmp3 = _mm_shuffle_epi32(H4, 78);
    tmp7 = _mm_shuffle_epi32(X4, 78);
    tmp3 = _mm_xor_si128(tmp3, H4);
    tmp7 = _mm_xor_si128(tmp7, X4);

    tmp0 = _mm_clmulepi64_si128(tmp0, tmp4, 0x00);
    tmp1 = _mm_clmulepi64_si128(tmp1, tmp5, 0x00);
    tmp2 = _mm_clmulepi64_si128(tmp2, tmp6, 0x00);
    tmp3 = _mm_clmulepi64_si128(tmp3, tmp7, 0x00);

    tmp0 = _mm_xor_si128(tmp0,  lo);
    tmp0 = _mm_xor_si128(tmp0,  hi);
    tmp0 = _mm_xor_si128(tmp1,  tmp0);
    tmp0 = _mm_xor_si128(tmp2,  tmp0);
    tmp0 = _mm_xor_si128(tmp3,  tmp0);

    tmp4 = _mm_slli_si128(tmp0, 8);
    tmp0 = _mm_srli_si128(tmp0, 8);

    lo = _mm_xor_si128(tmp4,  lo);
    hi = _mm_xor_si128(tmp0,  hi);

    tmp3 = lo;
    tmp6 = hi;

    tmp7 = _mm_srli_epi32(tmp3, 31);
    tmp8 = _mm_srli_epi32(tmp6, 31);
    tmp3 = _mm_slli_epi32(tmp3, 1);
    tmp6 = _mm_slli_epi32(tmp6, 1);

    tmp9 = _mm_srli_si128(tmp7, 12);
    tmp8 = _mm_slli_si128(tmp8, 4);
    tmp7 = _mm_slli_si128(tmp7, 4);
    tmp3 = _mm_or_si128(tmp3, tmp7);
    tmp6 = _mm_or_si128(tmp6, tmp8);
    tmp6 = _mm_or_si128(tmp6, tmp9);

    tmp7 = _mm_slli_epi32(tmp3, 31);
    tmp8 = _mm_slli_epi32(tmp3, 30);
    tmp9 = _mm_slli_epi32(tmp3, 25);

    tmp7 = _mm_xor_si128(tmp7, tmp8);
    tmp7 = _mm_xor_si128(tmp7, tmp9);
    tmp8 = _mm_srli_si128(tmp7, 4);
    tmp7 = _mm_slli_si128(tmp7, 12);
    tmp3 = _mm_xor_si128(tmp3, tmp7);

    tmp2 = _mm_srli_epi32(tmp3, 1);
    tmp4 = _mm_srli_epi32(tmp3, 2);
    tmp5 = _mm_srli_epi32(tmp3, 7);
    tmp2 = _mm_xor_si128(tmp2, tmp4);
    tmp2 = _mm_xor_si128(tmp2, tmp5);
    tmp2 = _mm_xor_si128(tmp2, tmp8);
```

```
    tmp3 = _mm_xor_si128(tmp3, tmp2);
    tmp6 = _mm_xor_si128(tmp6, tmp3);

    *res = tmp6;
    }
```

Code Examples: AES128-GCM

This chapter provides several code examples for implementing AES-GCM using PCLMULQDQ and the AES instructions (see [16] for details). We demonstrate here AES128 in GCM mode. The extension to AES192 and AES256 in GCM mode is straightforward (implementation of AES192/AES256 CTR is given in [16]). One of the AES-CTR implementations (Figure 12) uses the technique of processing several (four in this case) blocks in parallel. Reference [17] described the motivation and benefits of such parallelization techniques for AES in any parallel modes of operation.

How to Use the Code Examples

In the following, we provide three possible options for using the provided code examples.

For AES-GCM, using the simplest method (one blocks at a time): save Figure 5 as gfmul.c or, alternatively, Figure 6 as gfmul.s. Save Figure 9 as aes_gcm.c.

For AES-GCM, using the reflected variation, use Figure 7 for gfmul.c, and Figure 10 for aes_gcm.c.

For AES-GCM, using the parallelized method, save Figure 5 and Figure 8 together as gfmul.c, save Figure 11. as aes_gcm.c.

For all methods, save Figure 12 as key_schedule.c and Figure 13 as gcm_main.c.

For Intel Compiler (icc) users: the files can be compiled using the compilation line:

```
icc gcm.c key_schedule.c gcm_main.c gfmul.c  -o AES128_GCM -DTEST[1-6]
```

For gcc users: the files can be compiled using the compilation line

```
gcc -maes -msse4 key_schedule.c gcm_main.c gfmul.c  -o AES128_GCM -
DTEST[1-6]
```

-DTEST[1-6] selects one of the 6 AES GCM tests that are including in the main funrcion. Running the resulting executable (AES128_GCM) would give the respective printout, as described in the section "Code Outputs" below (e.g., -DTEST1 selects test number 1). The test vectors were taken from the specification document: http://csrc.nist.gov/groups/ST/toolkit/BCM/documents/proposedmodes/gcm/gcm-spec.pdf

The code can be run even without a processor based on Intel microarchitecture codename Westmere, using Intel® Software Development Emulator (Intel® SDE), which can be downloaded from http://www.intel.com/software/sde.

AES-GCM Code Examples

Figure 9. AES-GCM – Encrypt With Single Block Ghash at a Time

```
#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>

extern void gfmul(__m128i a,__m128i b,__m128i* c); //must be implemented elsewhere

void AES_GCM_encrypt(const unsigned char *in,
                     unsigned char *out,
                     const unsigned char* addt,
                     const unsigned char* ivec,
                     unsigned char *tag,
                     int nbytes,
                     int abytes,
                     int ibytes,
                     const unsigned char* key,
                     int nr)
    {
    int i, j ,k;
    __m128i hlp1, hlp2, hlp3, hlp4;
    __m128i tmp1, tmp2, tmp3, tmp4;
    __m128i H, Y, T;
    __m128i *KEY = (__m128i*)key;
    __m128i ctr1, ctr2, ctr3, ctr4;
    __m128i last_block = _mm_setzero_si128();
    __m128i ONE = _mm_set_epi32(0, 1, 0, 0);
    __m128i FOUR = _mm_set_epi32(0, 4, 0, 0);
    __m128i BSWAP_EPI64 = _mm_set_epi8(8, 9, 10, 11, 12, 13, 14, 15, 0, 1, 2, 3, 4, 5,
6, 7);
    __m128i BSWAP_MASK = _mm_set_epi8(0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13,
14, 15);
    __m128i X = _mm_setzero_si128();

    if(ibytes == 96/8){
        Y = _mm_loadu_si128((__m128i*)ivec);
        Y = _mm_insert_epi32(Y, 0x1000000, 3);
        /*(Compute E[ZERO, KS] and E[Y0, KS] together*/
        tmp1 = _mm_xor_si128(X, KEY[0]);
        tmp2 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr-1; j+=2) {
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);

             tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
             };
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);

        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        T = _mm_aesenclast_si128(tmp2, KEY[nr]);

        H = _mm_shuffle_epi8(H, BSWAP_MASK);
```

```
        }
    else{
        tmp1 = _mm_xor_si128(X, KEY[0]);
        for(j=1; j <nr; j++)
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        H = _mm_shuffle_epi8(H, BSWAP_MASK);
        Y = _mm_xor_si128(Y, Y);

        for(i=0; i < ibytes/16; i++){
            tmp1 = _mm_loadu_si128(&((__m128i*)ivec)[i]);
            tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        if(ibytes%16){
            for(j=0; j < ibytes%16; j++)
                ((unsigned char*)&last_block)[j] = ivec[i*16+j];
            tmp1 = last_block;
            tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        tmp1 = _mm_insert_epi64(tmp1, ibytes*8, 0);
        tmp1 = _mm_insert_epi64(tmp1, 0, 1);

        Y = _mm_xor_si128(Y, tmp1);
        gfmul(Y, H, &Y);
        Y = _mm_shuffle_epi8(Y, BSWAP_MASK);
        /*Compute E(K, Y0)*/
        tmp1 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr; j++)
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        T = _mm_aesenclast_si128(tmp1, KEY[nr]);
    }

    for(i=0; i<abytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)addt)[i]);
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    if(abytes%16){
        last_block = _mm_setzero_si128();
        for(j=0; j<abytes%16; j++)
            ((unsigned char*)&last_block)[j] = addt[i*16+j];
        tmp1 = last_block;
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }

    ctr1 = _mm_shuffle_epi8(Y, BSWAP_EPI64);
    ctr1 = _mm_add_epi64(ctr1, ONE);
    ctr2 = _mm_add_epi64(ctr1, ONE);
    ctr3 = _mm_add_epi64(ctr2, ONE);
    ctr4 = _mm_add_epi64(ctr3, ONE);
```

```
    for(i=0; i < nbytes/16/4; i++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp2 = _mm_shuffle_epi8(ctr2, BSWAP_EPI64);
        tmp3 = _mm_shuffle_epi8(ctr3, BSWAP_EPI64);
        tmp4 = _mm_shuffle_epi8(ctr4, BSWAP_EPI64);

        ctr1 = _mm_add_epi64(ctr1, FOUR);
        ctr2 = _mm_add_epi64(ctr2, FOUR);
        ctr3 = _mm_add_epi64(ctr3, FOUR);
        ctr4 = _mm_add_epi64(ctr4, FOUR);

        tmp1 =_mm_xor_si128(tmp1, KEY[0]);
        tmp2 =_mm_xor_si128(tmp2, KEY[0]);
        tmp3 =_mm_xor_si128(tmp3, KEY[0]);
        tmp4 =_mm_xor_si128(tmp4, KEY[0]);

        for(j=1; j < nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j]);

            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j+1]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j+1]);
            }

        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);
        tmp3 = _mm_aesenc_si128(tmp3, KEY[nr-1]);
        tmp4 = _mm_aesenc_si128(tmp4, KEY[nr-1]);

        tmp1 =_mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp2 =_mm_aesenclast_si128(tmp2, KEY[nr]);
        tmp3 =_mm_aesenclast_si128(tmp3, KEY[nr]);
        tmp4 =_mm_aesenclast_si128(tmp4, KEY[nr]);

        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[i*4+0]));
        tmp2 = _mm_xor_si128(tmp2, _mm_loadu_si128(&((__m128i*)in)[i*4+1]));
        tmp3 = _mm_xor_si128(tmp3, _mm_loadu_si128(&((__m128i*)in)[i*4+2]));
        tmp4 = _mm_xor_si128(tmp4, _mm_loadu_si128(&((__m128i*)in)[i*4+3]));

        _mm_storeu_si128(&((__m128i*)out)[i*4+0], tmp1);
        _mm_storeu_si128(&((__m128i*)out)[i*4+1], tmp2);
        _mm_storeu_si128(&((__m128i*)out)[i*4+2], tmp3);
        _mm_storeu_si128(&((__m128i*)out)[i*4+3], tmp4);

        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        tmp2 = _mm_shuffle_epi8(tmp2, BSWAP_MASK);
        tmp3 = _mm_shuffle_epi8(tmp3, BSWAP_MASK);
        tmp4 = _mm_shuffle_epi8(tmp4, BSWAP_MASK);

        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
```

```
        X = _mm_xor_si128(X, tmp2);
        gfmul(X, H, &X);
        X = _mm_xor_si128(X, tmp3);
        gfmul(X, H, &X);
        X = _mm_xor_si128(X, tmp4);
        gfmul(X, H, &X);
        }
    for(k = i*4; k < nbytes/16; k++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        ctr1 = _mm_add_epi64(ctr1, ONE);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        _mm_storeu_si128(&((__m128i*)out)[k], tmp1);
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X =_mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
//If one partial block remains
    if(nbytes%16){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        last_block = tmp1;
        for(j=0; j < nbytes%16; j++)
            out[k*16+j]=((unsigned char*)&last_block)[j];
        for(j; j<16; j++)
            ((unsigned char*)&last_block)[j]=0;
        tmp1 = last_block;
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X =_mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    tmp1 = _mm_insert_epi64(tmp1, nbytes*8, 0);
    tmp1 = _mm_insert_epi64(tmp1, abytes*8, 1);

    X = _mm_xor_si128(X, tmp1);
    gfmul(X, H, &X);
    X = _mm_shuffle_epi8(X, BSWAP_MASK);
    T = _mm_xor_si128(X, T);
    _mm_storeu_si128((__m128i*)tag, T);
}
```

Figure 10. AES-GCM – Decrypt With Single Block Ghash at a Time

```
#include <wmmintrin.h>
```

```
#include <emmintrin.h>
#include <smmintrin.h>

extern void gfmul(__m128i a,__m128i b,__m128i* c); //must be implemented elsewhere

int AES_GCM_decrypt (const unsigned char *in,
                     unsigned char *out,
                     const unsigned char* addt,
                     const unsigned char* ivec,
                     unsigned char *tag,
                     int nbytes,
                     int abytes,
                     int ibytes,
                     const unsigned char* key,
                     int nr)
    {
    int i, j ,k;
    __m128i hlp1, hlp2, hlp3, hlp4;
    __m128i tmp1, tmp2, tmp3, tmp4;
    __m128i H, Y, T;
    __m128i *KEY = (__m128i*)key;
    __m128i ctr1, ctr2, ctr3, ctr4;
    __m128i last_block = _mm_setzero_si128();
    __m128i ONE = _mm_set_epi32(0, 1, 0, 0);
    __m128i FOUR = _mm_set_epi32(0, 4, 0, 0);
    __m128i BSWAP_EPI64 = _mm_set_epi8(8,9,10,11,12,13,14,15,0,1,2,3,4,5,6,7);
    __m128i BSWAP_MASK = _mm_set_epi8(0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15);
    __m128i X = _mm_setzero_si128();

    if(ibytes == 96/8){
        Y = _mm_loadu_si128((__m128i*)ivec);
        Y = _mm_insert_epi32(Y, 0x1000000, 3);
        /*(Compute E[ZERO, KS] and E[Y0, KS] together*/
        tmp1 = _mm_xor_si128(X, KEY[0]);
        tmp2 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr-1; j+=2) {
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);

             tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
             };
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);

        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        T = _mm_aesenclast_si128(tmp2, KEY[nr]);

        H = _mm_shuffle_epi8(H, BSWAP_MASK);
        }
    else{
        tmp1 = _mm_xor_si128(X, KEY[0]);
        for(j=1; j <nr; j++)
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        H = _mm_shuffle_epi8(H, BSWAP_MASK);
        Y = _mm_xor_si128(Y, Y);
```

```
        for(i=0; i < ibytes/16; i++){
            tmp1 = _mm_loadu_si128(&((__m128i*)ivec)[i]);
            tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        if(ibytes%16){
            for(j=0; j < ibytes%16; j++)
                ((unsigned char*)&last_block)[j] = ivec[i*16+j];
            tmp1 = last_block;
            tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        tmp1 = _mm_insert_epi64(tmp1, ibytes*8, 0);
        tmp1 = _mm_insert_epi64(tmp1, 0, 1);

        Y = _mm_xor_si128(Y, tmp1);
        gfmul(Y, H, &Y);
        Y = _mm_shuffle_epi8(Y, BSWAP_MASK);
        /*Compute E(K, Y0)*/
        tmp1 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr; j++)
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        T = _mm_aesenclast_si128(tmp1, KEY[nr]);
    }

    for(i=0; i<abytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)addt)[i]);
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    if(abytes%16){
        last_block = _mm_setzero_si128();
        for(j=0;j<abytes%16;j++)
            ((unsigned char*)&last_block)[j] = addt[i*16+j];
        tmp1 = last_block;
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X =_mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }

    for(i=0; i<nbytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)in)[i]);
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    if(nbytes%16){
        last_block = _mm_setzero_si128();
        for(j=0; j<nbytes%16; j++)
            ((unsigned char*)&last_block)[j] = addt[i*16+j];
        tmp1 = last_block;
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
```

```
        gfmul(X, H, &X);
        }

    tmp1 =_mm_insert_epi64(tmp1, nbytes*8, 0);
    tmp1 =_mm_insert_epi64(tmp1, abytes*8, 1);

    X = _mm_xor_si128(X, tmp1);
    gfmul(X, H, &X);
    X = _mm_shuffle_epi8(X, BSWAP_MASK);
    T = _mm_xor_si128(X, T);

    if(_mm_testz_si128(T, _mm_loadu_si128((__m128i*)tag)))
        return 0;   //in case the authentication failed

    ctr1 = _mm_shuffle_epi8(Y, BSWAP_EPI64);
    ctr1 = _mm_add_epi64(ctr1, ONE);
    ctr2 = _mm_add_epi64(ctr1, ONE);
    ctr3 = _mm_add_epi64(ctr2, ONE);
    ctr4 = _mm_add_epi64(ctr3, ONE);

    for(i=0; i < nbytes/16/4; i++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp2 = _mm_shuffle_epi8(ctr2, BSWAP_EPI64);
        tmp3 = _mm_shuffle_epi8(ctr3, BSWAP_EPI64);
        tmp4 = _mm_shuffle_epi8(ctr4, BSWAP_EPI64);

        ctr1 = _mm_add_epi64(ctr1, FOUR);
        ctr2 = _mm_add_epi64(ctr2, FOUR);
        ctr3 = _mm_add_epi64(ctr3, FOUR);
        ctr4 = _mm_add_epi64(ctr4, FOUR);

        tmp1 =_mm_xor_si128(tmp1, KEY[0]);
        tmp2 =_mm_xor_si128(tmp2, KEY[0]);
        tmp3 =_mm_xor_si128(tmp3, KEY[0]);
        tmp4 =_mm_xor_si128(tmp4, KEY[0]);

        for(j=1; j < nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j]);

            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j+1]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j+1]);
            }

        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);
        tmp3 = _mm_aesenc_si128(tmp3, KEY[nr-1]);
        tmp4 = _mm_aesenc_si128(tmp4, KEY[nr-1]);

        tmp1 =_mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp2 =_mm_aesenclast_si128(tmp2, KEY[nr]);
        tmp3 =_mm_aesenclast_si128(tmp3, KEY[nr]);
```

```
        tmp4 =_mm_aesenclast_si128(tmp4, KEY[nr]);

        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[i*4+0]));
        tmp2 = _mm_xor_si128(tmp2, _mm_loadu_si128(&((__m128i*)in)[i*4+1]));
        tmp3 = _mm_xor_si128(tmp3, _mm_loadu_si128(&((__m128i*)in)[i*4+2]));
        tmp4 = _mm_xor_si128(tmp4, _mm_loadu_si128(&((__m128i*)in)[i*4+3]));

        _mm_storeu_si128(&((__m128i*)out)[i*4+0], tmp1);
        _mm_storeu_si128(&((__m128i*)out)[i*4+1], tmp2);
        _mm_storeu_si128(&((__m128i*)out)[i*4+2], tmp3);
        _mm_storeu_si128(&((__m128i*)out)[i*4+3], tmp4);

        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        tmp2 = _mm_shuffle_epi8(tmp2, BSWAP_MASK);
        tmp3 = _mm_shuffle_epi8(tmp3, BSWAP_MASK);
        tmp4 = _mm_shuffle_epi8(tmp4, BSWAP_MASK);
        }
    for(k = i*4; k < nbytes/16; k++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        ctr1 = _mm_add_epi64(ctr1, ONE);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        _mm_storeu_si128(&((__m128i*)out)[k], tmp1);
        }
//If one partial block remains
    if(nbytes%16){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 =_mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 =_mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        last_block = tmp1;
        for(j=0; j<nbytes%16; j++)
            out[k*16+j]=((unsigned char*)&last_block)[j];
        }
    return 1; //when sucessfull returns 1
}
```

Figure 11. AES-GCM – One Block at a Time with Bit Reflection (to Be Used with the Multiplication Function from Figure 7).

```
#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>

#define REFLECT(X)\
```

```
    hlp1 = _mm_srli_epi16(X,4);\
    X = _mm_and_si128(AMASK,X);\
    hlp1 = _mm_and_si128(AMASK,hlp1);\
    X = _mm_shuffle_epi8(MASKH,X);\
    hlp1 = _mm_shuffle_epi8(MASKL,hlp1);\
    X = _mm_xor_si128(X,hlp1)

extern void gfmul(__m128i a,__m128i b,__m128i* c); //must be implemented elsewhere

void AES_GCM_encrypt(const unsigned char *in,
                     unsigned char *out,
                     const unsigned char* addt,
                     const unsigned char* ivec,
                     unsigned char *tag,
                     int nbytes,
                     int abytes,
                     int ibytes,
                     const unsigned char* key,
                     int nr)
    {
    int i, j ,k;
    __m128i hlp1, hlp2, hlp3, hlp4;
    __m128i tmp1, tmp2, tmp3, tmp4;
    __m128i H, Y, T;
    __m128i *KEY = (__m128i*)key;
    __m128i ctr1, ctr2, ctr3, ctr4;
    __m128i last_block = _mm_setzero_si128();
    __m128i ONE = _mm_set_epi32(0, 1, 0, 0);
    __m128i FOUR = _mm_set_epi32(0, 4, 0, 0);
    __m128i BSWAP_EPI64 = _mm_set_epi8(8, 9, 10, 11, 12, 13, 14, 15, 0, 1, 2, 3, 4, 5,
6, 7);
    __m128i BSWAP_MASK = _mm_set_epi8(0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13,
14, 15);
    __m128i X = _mm_setzero_si128();
    __m128i AMASK = _mm_set_epi32(0x0f0f0f0f, 0x0f0f0f0f, 0x0f0f0f0f, 0x0f0f0f0f);
    __m128i MASKL = _mm_set_epi32(0x0f070b03, 0x0d050901, 0x0e060a02, 0x0c040800);
    __m128i MASKH = _mm_set_epi32(0xf070b030, 0xd0509010, 0xe060a020, 0xc0408000);
    __m128i MASKF = _mm_set_epi32(0x00010203, 0x04050607, 0x08090a0b, 0x0c0d0e0f);

    if(ibytes == 96/8){
        Y = _mm_loadu_si128((__m128i*)ivec);
        Y = _mm_insert_epi32(Y, 0x1000000, 3);
        /*(Compute E[ZERO, KS] and E[Y0, KS] together*/
        tmp1 = _mm_xor_si128(X, KEY[0]);
        tmp2 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr-1; j+=2) {
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);

             tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
             };
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);

        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        T = _mm_aesenclast_si128(tmp2, KEY[nr]);
```

```
        REFLECT(H);
        }
    else{
        tmp1 = _mm_xor_si128(X, KEY[0]);
        for(j=1; j < nr; j++)
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        REFLECT(H);
        Y = _mm_xor_si128(Y, Y);

        for(i=0; i < ibytes/16; i++){
            tmp1 = _mm_loadu_si128(&((__m128i*)ivec)[i]);
            REFLECT(tmp1);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        if(ibytes%16){
            for(j=0; j < ibytes%16; j++)
                ((unsigned char*)&last_block)[j] = ivec[i*16+j];
            tmp1 = last_block;
            REFLECT(tmp1);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        tmp1 = _mm_insert_epi64(tmp1, ibytes*8, 0);
        tmp1 = _mm_insert_epi64(tmp1, 0, 1);
        REFLECT(tmp1);
        tmp1 = _mm_shuffle_epi8(tmp1, MASKF);
        Y = _mm_xor_si128(Y, tmp1);
        gfmul(Y, H, &Y);
        REFLECT(Y);
        /*Compute E(K, Y0)*/
        tmp1 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr; j++)
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        T = _mm_aesenclast_si128(tmp1, KEY[nr]);
    }

    for(i=0; i<abytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)addt)[i]);
        REFLECT(tmp1);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    if(abytes%16){
        last_block = _mm_setzero_si128();
        for(j=0; j<abytes%16; j++)
            ((unsigned char*)&last_block)[j] = addt[i*16+j];
        tmp1 = last_block;
        REFLECT(tmp1);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }

    ctr1 = _mm_shuffle_epi8(Y, BSWAP_EPI64);
    ctr1 = _mm_add_epi64(ctr1, ONE);
    ctr2 = _mm_add_epi64(ctr1, ONE);
```

```
    ctr3 = _mm_add_epi64(ctr2, ONE);
    ctr4 = _mm_add_epi64(ctr3, ONE);

    for(i=0; i < nbytes/16/4; i++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp2 = _mm_shuffle_epi8(ctr2, BSWAP_EPI64);
        tmp3 = _mm_shuffle_epi8(ctr3, BSWAP_EPI64);
        tmp4 = _mm_shuffle_epi8(ctr4, BSWAP_EPI64);

        ctr1 = _mm_add_epi64(ctr1, FOUR);
        ctr2 = _mm_add_epi64(ctr2, FOUR);
        ctr3 = _mm_add_epi64(ctr3, FOUR);
        ctr4 = _mm_add_epi64(ctr4, FOUR);

        tmp1 =_mm_xor_si128(tmp1, KEY[0]);
        tmp2 =_mm_xor_si128(tmp2, KEY[0]);
        tmp3 =_mm_xor_si128(tmp3, KEY[0]);
        tmp4 =_mm_xor_si128(tmp4, KEY[0]);

        for(j=1; j < nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j]);

            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j+1]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j+1]);
            }

        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);
        tmp3 = _mm_aesenc_si128(tmp3, KEY[nr-1]);
        tmp4 = _mm_aesenc_si128(tmp4, KEY[nr-1]);

        tmp1 =_mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp2 =_mm_aesenclast_si128(tmp2, KEY[nr]);
        tmp3 =_mm_aesenclast_si128(tmp3, KEY[nr]);
        tmp4 =_mm_aesenclast_si128(tmp4, KEY[nr]);

        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[i*4+0]));
        tmp2 = _mm_xor_si128(tmp2, _mm_loadu_si128(&((__m128i*)in)[i*4+1]));
        tmp3 = _mm_xor_si128(tmp3, _mm_loadu_si128(&((__m128i*)in)[i*4+2]));
        tmp4 = _mm_xor_si128(tmp4, _mm_loadu_si128(&((__m128i*)in)[i*4+3]));

        _mm_storeu_si128(&((__m128i*)out)[i*4+0], tmp1);
        _mm_storeu_si128(&((__m128i*)out)[i*4+1], tmp2);
        _mm_storeu_si128(&((__m128i*)out)[i*4+2], tmp3);
        _mm_storeu_si128(&((__m128i*)out)[i*4+3], tmp4);

        REFLECT(tmp1);
        REFLECT(tmp2);
        REFLECT(tmp3);
        REFLECT(tmp4);
```

```
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        X = _mm_xor_si128(X, tmp2);
        gfmul(X, H, &X);
        X = _mm_xor_si128(X, tmp3);
        gfmul(X, H, &X);
        X = _mm_xor_si128(X, tmp4);
        gfmul(X, H, &X);
        }
    for(k = i*4; k < nbytes/16; k++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        ctr1 = _mm_add_epi64(ctr1, ONE);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        _mm_storeu_si128(&((__m128i*)out)[k], tmp1);
        REFLECT(tmp1);
        X =_mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
//If one partial block remains
    if(nbytes%16){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        last_block = tmp1;
        for(j=0; j < nbytes%16; j++)
            out[k*16+j]=((unsigned char*)&last_block)[j];
        for(j; j<16; j++)
            ((unsigned char*)&last_block)[j]=0;
        tmp1 = last_block;
        REFLECT(tmp1);
        X =_mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    tmp1 = _mm_insert_epi64(tmp1, nbytes*8, 0);
    tmp1 = _mm_insert_epi64(tmp1, abytes*8, 1);
    REFLECT(tmp1);
    tmp1 = _mm_shuffle_epi8(tmp1, MASKF);
    X = _mm_xor_si128(X, tmp1);
    gfmul(X, H, &X);
    REFLECT(X);
    T = _mm_xor_si128(X, T);
    _mm_storeu_si128((__m128i*)tag, T);
}
```

```
int AES_GCM_decrypt (const unsigned char *in,
                     unsigned char *out,
                     const unsigned char* addt,
                     const unsigned char* ivec,
                     unsigned char *tag,
                     int nbytes,
                     int abytes,
                     int ibytes,
                     const unsigned char* key,
                     int nr)
    {
    int i, j ,k;
    __m128i hlp1, hlp2, hlp3, hlp4;
    __m128i tmp1, tmp2, tmp3, tmp4;
    __m128i H, Y, T;
    __m128i *KEY = (__m128i*)key;
    __m128i ctr1, ctr2, ctr3, ctr4;
    __m128i last_block = _mm_setzero_si128();
    __m128i ONE = _mm_set_epi32(0, 1, 0, 0);
    __m128i FOUR = _mm_set_epi32(0, 4, 0, 0);
    __m128i BSWAP_EPI64 = _mm_set_epi8(8, 9, 10, 11, 12, 13, 14, 15, 0, 1, 2, 3, 4, 5,
6, 7);
    __m128i BSWAP_MASK = _mm_set_epi8(0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13,
14, 15);
    __m128i X = _mm_setzero_si128();
    __m128i AMASK = _mm_set_epi32(0x0f0f0f0f, 0x0f0f0f0f, 0x0f0f0f0f, 0x0f0f0f0f);
    __m128i MASKL = _mm_set_epi32(0x0f070b03, 0x0d050901, 0x0e060a02, 0x0c040800);
    __m128i MASKH = _mm_set_epi32(0xf070b030, 0xd0509010, 0xe060a020, 0xc0408000);
    __m128i MASKF = _mm_set_epi32(0x00010203, 0x04050607, 0x08090a0b, 0x0c0d0e0f);

    if(ibytes == 96/8){
        Y = _mm_loadu_si128((__m128i*)ivec);
        Y = _mm_insert_epi32(Y, 0x1000000, 3);
        /*(Compute E[ZERO, KS] and E[Y0, KS] together*/
        tmp1 = _mm_xor_si128(X, KEY[0]);
        tmp2 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr-1; j+=2) {
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);

             tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
             };
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);

        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        T = _mm_aesenclast_si128(tmp2, KEY[nr]);

        REFLECT(H);
        }
    else{
        tmp1 = _mm_xor_si128(X, KEY[0]);
        for(j=1; j < nr; j++)
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
```

```
        REFLECT(H);
        Y = _mm_xor_si128(Y, Y);

        for(i=0; i < ibytes/16; i++){
            tmp1 = _mm_loadu_si128(&((__m128i*)ivec)[i]);
            REFLECT(tmp1);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        if(ibytes%16){
            for(j=0; j < ibytes%16; j++)
                ((unsigned char*)&last_block)[j] = ivec[i*16+j];
            tmp1 = last_block;
            REFLECT(tmp1);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        tmp1 = _mm_insert_epi64(tmp1, ibytes*8, 0);
        tmp1 = _mm_insert_epi64(tmp1, 0, 1);
        REFLECT(tmp1);
        tmp1 = _mm_shuffle_epi8(tmp1, MASKF);
        Y = _mm_xor_si128(Y, tmp1);
        gfmul(Y, H, &Y);
        REFLECT(Y);
        /*Compute E(K, Y0)*/
        tmp1 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr; j++)
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        T = _mm_aesenclast_si128(tmp1, KEY[nr]);
    }

    for(i=0; i<abytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)addt)[i]);
        REFLECT(tmp1);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    if(abytes%16){
        last_block = _mm_setzero_si128();
        for(j=0; j<abytes%16; j++)
            ((unsigned char*)&last_block)[j] = addt[i*16+j];
        tmp1 = last_block;
        REFLECT(tmp1);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }

    for(i=0; i<nbytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)in)[i]);
        REFLECT(tmp1);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    if(nbytes%16){
        last_block = _mm_setzero_si128();
        for(j=0; j<nbytes%16; j++)
            ((unsigned char*)&last_block)[j] = in[i*16+j];
        tmp1 = last_block;
```

```
        REFLECT(tmp1);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }

    tmp1 = _mm_insert_epi64(tmp1, nbytes*8, 0);
    tmp1 = _mm_insert_epi64(tmp1, abytes*8, 1);
    REFLECT(tmp1);
    tmp1 = _mm_shuffle_epi8(tmp1, MASKF);
    X = _mm_xor_si128(X, tmp1);
    gfmul(X, H, &X);
    REFLECT(X);
    T = _mm_xor_si128(X, T);

    if(_mm_testz_si128(T, _mm_loadu_si128((__m128i*)tag)))
        return 0;   //in case the authentication failed

    ctr1 = _mm_shuffle_epi8(Y, BSWAP_EPI64);
    ctr1 = _mm_add_epi64(ctr1, ONE);
    ctr2 = _mm_add_epi64(ctr1, ONE);
    ctr3 = _mm_add_epi64(ctr2, ONE);
    ctr4 = _mm_add_epi64(ctr3, ONE);

    for(i=0; i < nbytes/16/4; i++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp2 = _mm_shuffle_epi8(ctr2, BSWAP_EPI64);
        tmp3 = _mm_shuffle_epi8(ctr3, BSWAP_EPI64);
        tmp4 = _mm_shuffle_epi8(ctr4, BSWAP_EPI64);

        ctr1 = _mm_add_epi64(ctr1, FOUR);
        ctr2 = _mm_add_epi64(ctr2, FOUR);
        ctr3 = _mm_add_epi64(ctr3, FOUR);
        ctr4 = _mm_add_epi64(ctr4, FOUR);

        tmp1 =_mm_xor_si128(tmp1, KEY[0]);
        tmp2 =_mm_xor_si128(tmp2, KEY[0]);
        tmp3 =_mm_xor_si128(tmp3, KEY[0]);
        tmp4 =_mm_xor_si128(tmp4, KEY[0]);

        for(j=1; j < nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j]);

            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j+1]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j+1]);
            }

        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);
        tmp3 = _mm_aesenc_si128(tmp3, KEY[nr-1]);
        tmp4 = _mm_aesenc_si128(tmp4, KEY[nr-1]);
```

```
        tmp1 =_mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp2 =_mm_aesenclast_si128(tmp2, KEY[nr]);
        tmp3 =_mm_aesenclast_si128(tmp3, KEY[nr]);
        tmp4 =_mm_aesenclast_si128(tmp4, KEY[nr]);

        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[i*4+0]));
        tmp2 = _mm_xor_si128(tmp2, _mm_loadu_si128(&((__m128i*)in)[i*4+1]));
        tmp3 = _mm_xor_si128(tmp3, _mm_loadu_si128(&((__m128i*)in)[i*4+2]));
        tmp4 = _mm_xor_si128(tmp4, _mm_loadu_si128(&((__m128i*)in)[i*4+3]));

        _mm_storeu_si128(&((__m128i*)out)[i*4+0], tmp1);
        _mm_storeu_si128(&((__m128i*)out)[i*4+1], tmp2);
        _mm_storeu_si128(&((__m128i*)out)[i*4+2], tmp3);
        _mm_storeu_si128(&((__m128i*)out)[i*4+3], tmp4);

        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        tmp2 = _mm_shuffle_epi8(tmp2, BSWAP_MASK);
        tmp3 = _mm_shuffle_epi8(tmp3, BSWAP_MASK);
        tmp4 = _mm_shuffle_epi8(tmp4, BSWAP_MASK);
        }
    for(k = i*4; k < nbytes/16; k++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        ctr1 = _mm_add_epi64(ctr1, ONE);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        _mm_storeu_si128(&((__m128i*)out)[k], tmp1);
        }
//If one partial block remains
    if(nbytes%16){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 =_mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 =_mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        last_block = tmp1;
        for(j=0; j<nbytes%16; j++)
            out[k*16+j]=((unsigned char*)&last_block)[j];
        }
    return 1; //when sucessfull returns 1
}
```

Figure 12. AES-GCM: Processing Four Blocks in Parallel with Aggregated Every Four Blocks

```
#include <wmmintrin.h>
#include <emmintrin.h>
```

```
#include <smmintrin.h>

extern void gfmul(__m128i a,__m128i b,__m128i* c); //must be implemented elsewhere

extern void reduce4 (__m128i H1,__m128i H2,__m128i H3,__m128i H4,
              __m128i X1,__m128i X2,__m128i X3, __m128i X4, __m128i *res);

void AES_GCM_encrypt(const unsigned char *in,
                     unsigned char *out,
                     const unsigned char* addt,
                     const unsigned char* ivec,
                     unsigned char *tag,
                     int nbytes,
                     int abytes,
                     int ibytes,
                     const unsigned char* key,
                     int nr)
    {
    int i, j ,k;
    __m128i hlp1, hlp2, hlp3, hlp4;
    __m128i tmp1, tmp2, tmp3, tmp4;
    __m128i H, H1, H2, H3, H4, Y, T;
    __m128i *KEY = (__m128i*)key;
    __m128i ctr1, ctr2, ctr3, ctr4;
    __m128i last_block = _mm_setzero_si128();
    __m128i ONE = _mm_set_epi32(0, 1, 0, 0);
    __m128i FOUR = _mm_set_epi32(0, 4, 0, 0);
    __m128i BSWAP_EPI64 = _mm_set_epi8(8,9,10,11,12,13,14,15,0,1,2,3,4,5,6,7);
    __m128i BSWAP_MASK = _mm_set_epi8(0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15);
    __m128i X = _mm_setzero_si128();

    if(ibytes == 96/8){
        Y = _mm_loadu_si128((__m128i*)ivec);
        Y = _mm_insert_epi32(Y, 0x1000000, 3);
        /*(Compute E[ZERO, KS] and E[Y0, KS] together*/
        tmp1 = _mm_xor_si128(X, KEY[0]);
        tmp2 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr-1; j+=2) {
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);

             tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
             tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
             };
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);

        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
        T = _mm_aesenclast_si128(tmp2, KEY[nr]);

        H = _mm_shuffle_epi8(H, BSWAP_MASK);
        }
    else{
        tmp1 = _mm_xor_si128(X, KEY[0]);
        for(j=1; j <nr; j++)
             tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        H = _mm_aesenclast_si128(tmp1, KEY[nr]);
```

```
        H = _mm_shuffle_epi8(H, BSWAP_MASK);
        Y = _mm_xor_si128(Y, Y);

        for(i=0; i < ibytes/16; i++){
            tmp1 = _mm_loadu_si128(&((__m128i*)ivec)[i]);
            tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        if(ibytes%16){
            for(j=0; j < ibytes%16; j++)
                ((unsigned char*)&last_block)[j] = ivec[i*16+j];
            tmp1 = last_block;
            tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
            Y = _mm_xor_si128(Y, tmp1);
            gfmul(Y, H, &Y);
            }
        tmp1 = _mm_insert_epi64(tmp1, ibytes*8, 0);
        tmp1 = _mm_insert_epi64(tmp1, 0, 1);

        Y = _mm_xor_si128(Y, tmp1);
        gfmul(Y, H, &Y);
        Y = _mm_shuffle_epi8(Y, BSWAP_MASK);
        /*Compute E(K, Y0)*/
        tmp1 = _mm_xor_si128(Y, KEY[0]);
        for(j=1; j < nr; j++)
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
        T = _mm_aesenclast_si128(tmp1, KEY[nr]);
    }

    gfmul(H,H,&H2);
    gfmul(H,H2,&H3);
    gfmul(H,H3,&H4);

    for(i=0; i<abytes/16/4; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)addt)[i*4]);
        tmp2 = _mm_loadu_si128(&((__m128i*)addt)[i*4+1]);
        tmp3 = _mm_loadu_si128(&((__m128i*)addt)[i*4+2]);
        tmp4 = _mm_loadu_si128(&((__m128i*)addt)[i*4+3]);

        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        tmp2 = _mm_shuffle_epi8(tmp2, BSWAP_MASK);
        tmp3 = _mm_shuffle_epi8(tmp3, BSWAP_MASK);
        tmp4 = _mm_shuffle_epi8(tmp4, BSWAP_MASK);

        tmp1 = _mm_xor_si128(X, tmp1);

        reduce4(H, H2, H3, H4, tmp4, tmp3, tmp2, tmp1, &X);
        }
    for(i=i*4; i<abytes/16; i++){
        tmp1 = _mm_loadu_si128(&((__m128i*)addt)[i]);
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X,tmp1);
        gfmul(X, H, &X);
        }
    if(abytes%16){
        last_block = _mm_setzero_si128();
```

```
        for(j=0; j<abytes%16; j++)
            ((unsigned char*)&last_block)[j] = addt[i*16+j];
        tmp1 = last_block;
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X =_mm_xor_si128(X,tmp1);
        gfmul(X,H,&X);
        }

    ctr1 = _mm_shuffle_epi8(Y, BSWAP_EPI64);
    ctr1 = _mm_add_epi64(ctr1, ONE);
    ctr2 = _mm_add_epi64(ctr1, ONE);
    ctr3 = _mm_add_epi64(ctr2, ONE);
    ctr4 = _mm_add_epi64(ctr3, ONE);

    for(i=0; i<nbytes/16/4; i++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp2 = _mm_shuffle_epi8(ctr2, BSWAP_EPI64);
        tmp3 = _mm_shuffle_epi8(ctr3, BSWAP_EPI64);
        tmp4 = _mm_shuffle_epi8(ctr4, BSWAP_EPI64);

        ctr1 = _mm_add_epi64(ctr1, FOUR);
        ctr2 = _mm_add_epi64(ctr2, FOUR);
        ctr3 = _mm_add_epi64(ctr3, FOUR);
        ctr4 = _mm_add_epi64(ctr4, FOUR);

        tmp1 =_mm_xor_si128(tmp1, KEY[0]);
        tmp2 =_mm_xor_si128(tmp2, KEY[0]);
        tmp3 =_mm_xor_si128(tmp3, KEY[0]);
        tmp4 =_mm_xor_si128(tmp4, KEY[0]);

        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j]);

            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            tmp2 = _mm_aesenc_si128(tmp2, KEY[j+1]);
            tmp3 = _mm_aesenc_si128(tmp3, KEY[j+1]);
            tmp4 = _mm_aesenc_si128(tmp4, KEY[j+1]);
            }

        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp2 = _mm_aesenc_si128(tmp2, KEY[nr-1]);
        tmp3 = _mm_aesenc_si128(tmp3, KEY[nr-1]);
        tmp4 = _mm_aesenc_si128(tmp4, KEY[nr-1]);

        tmp1 =_mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp2 =_mm_aesenclast_si128(tmp2, KEY[nr]);
        tmp3 =_mm_aesenclast_si128(tmp3, KEY[nr]);
        tmp4 =_mm_aesenclast_si128(tmp4, KEY[nr]);

        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[i*4+0]));
        tmp2 = _mm_xor_si128(tmp2, _mm_loadu_si128(&((__m128i*)in)[i*4+1]));
        tmp3 = _mm_xor_si128(tmp3, _mm_loadu_si128(&((__m128i*)in)[i*4+2]));
        tmp4 = _mm_xor_si128(tmp4, _mm_loadu_si128(&((__m128i*)in)[i*4+3]));
```

```
        _mm_storeu_si128(&((__m128i*)out)[i*4+0], tmp1);
        _mm_storeu_si128(&((__m128i*)out)[i*4+1], tmp2);
        _mm_storeu_si128(&((__m128i*)out)[i*4+2], tmp3);
        _mm_storeu_si128(&((__m128i*)out)[i*4+3], tmp4);

        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        tmp2 = _mm_shuffle_epi8(tmp2, BSWAP_MASK);
        tmp3 = _mm_shuffle_epi8(tmp3, BSWAP_MASK);
        tmp4 = _mm_shuffle_epi8(tmp4, BSWAP_MASK);

        tmp1 = _mm_xor_si128(X, tmp1);

        reduce4(H, H2, H3, H4, tmp4, tmp3, tmp2, tmp1, &X);
        }
    for(k=i*4; k<nbytes/16; k++){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        ctr1 = _mm_add_epi64(ctr1, ONE);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        _mm_storeu_si128(&((__m128i*)out)[k], tmp1);
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X,H,&X);
        }
//If remains one incomplete block
    if(nbytes%16){
        tmp1 = _mm_shuffle_epi8(ctr1, BSWAP_EPI64);
        tmp1 = _mm_xor_si128(tmp1, KEY[0]);
        for(j=1; j<nr-1; j+=2){
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j]);
            tmp1 = _mm_aesenc_si128(tmp1, KEY[j+1]);
            }
        tmp1 = _mm_aesenc_si128(tmp1, KEY[nr-1]);
        tmp1 = _mm_aesenclast_si128(tmp1, KEY[nr]);
        tmp1 = _mm_xor_si128(tmp1, _mm_loadu_si128(&((__m128i*)in)[k]));
        last_block = tmp1;
        for(j=0; j<nbytes%16; j++)
            out[k*16+j] = ((unsigned char*)&last_block)[j];
        for(j; j<16; j++)
            ((unsigned char*)&last_block)[j] = 0;
        tmp1 = last_block;
        tmp1 = _mm_shuffle_epi8(tmp1, BSWAP_MASK);
        X = _mm_xor_si128(X, tmp1);
        gfmul(X, H, &X);
        }
    tmp1 = _mm_insert_epi64(tmp1, nbytes*8, 0);
    tmp1 = _mm_insert_epi64(tmp1, abytes*8, 1);

    X = _mm_xor_si128(X, tmp1);
    gfmul(X,H,&X);
```

```
    X = _mm_shuffle_epi8(X, BSWAP_MASK);
    T = _mm_xor_si128(X, T);
    _mm_storeu_si128((__m128i*)tag, T);
}
```

Figure 13. AES128 Key Expansion

```
inline void key_expansion_128(__m128i* temp1,
                              __m128i* temp2,
                                int KS_Pointer,
                              __m128i *Key_Schedule)
    {
    __m128i temp3;

    *temp2 = _mm_shuffle_epi32 (*temp2, 0xff);
    temp3  = _mm_slli_si128 (*temp1, 0x4);
    *temp1 = _mm_xor_si128 (*temp1, temp3);
    temp3  = _mm_slli_si128 (temp3, 0x4);
    *temp1 = _mm_xor_si128 (*temp1, temp3);
    temp3  = _mm_slli_si128 (temp3, 0x4);
    *temp1 = _mm_xor_si128 (*temp1, temp3);
    *temp1 = _mm_xor_si128 (*temp1, *temp2);

    Key_Schedule[KS_Pointer]=*temp1;
    }

void AES_128_Key_Expansion_unrolled (const uint8 *userkey,
                                     AES_KEY *key)
    {
    key->nr=10;

    m128i temp1, temp2, temp3;
    m128i *Key_Schedule=(__m128i*)key->KEY;
    int KS_Pointer=1;
    int i;

    temp1= _mm_loadu_si128((__m128i*)userkey);
    Key_Schedule[0]=temp1;

    temp2 = _mm_aeskeygenassist_si128 (temp1,0x1);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x2);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x4);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x8);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x10);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x20);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x40);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x80);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x1b);
```

```
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    temp2 = _mm_aeskeygenassist_si128 (temp1,0x36);
    key_expansion_128(&temp1, &temp2, KS_Pointer++, Key_Schedule);
    }
```

Figure 14. A Main Function for Testing

```
//#define TEST1
//#define TEST2
//#define TEST3
//#define TEST4
//#define TEST5
//#define TEST6
//#define CUSTOM_TEST

#include <wmmintrin.h>
#include <emmintrin.h>
#include <smmintrin.h>
#include <stdint.h>
#include <stdio.h>

#if !defined (ALIGN16)
# if defined (__GNUC__)
#  define ALIGN16  __attribute__  ( (aligned (16)))
# else
#  define ALIGN16 __declspec (align (16))
# endif
#endif

typedef struct KEY_SCHEDULE{
    ALIGN16 uint8_t KEY[16*15];
    int nr;
    }AES_KEY;

#define cpuid(func,ax,bx,cx,dx)\
           __asm__ __volatile__ ("cpuid":\
           "=a" (ax), "=b" (bx), "=c" (cx), "=d" (dx) : "a" (func));

int Check_CPU_support_AES()
    {
    unsigned int a,b,c,d;
    cpuid(1, a,b,c,d);
    return (c & 0x2000000);
    }

/****************************************************************************/
void print_m128i_with_string(char* string,__m128i data)
    {
    unsigned char *pointer = (unsigned char*)&data;
    int i;
    printf("%-40s[0x",string);
    for (i=0; i<16; i++)
        printf("%02x",pointer[i]);
    printf("]\n");
    }
void print_m128i_with_string_short(char* string,__m128i data,int length)
    {
    unsigned char *pointer = (unsigned char*)&data;
```

```
    int i;
    printf("%-40s[0x",string);
    for (i=0; i<length; i++)
        printf("%02x",pointer[i]);
    printf("]\n");
    }
/*****************************************************************************/
int main (){
//The test vectors are taken from:
//http://csrc.nist.gov/groups/ST/toolkit/BCM/documents/proposedmodes/gcm/gcm-spec.pdf
#ifdef TEST1
#define NBYTES 0
#define MBYTES 0
#define IBYTES 12
    ALIGN16 uint8_t K[16]={0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00,
                         0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00};
    ALIGN16 uint8_t P[NBYTES]={};
    ALIGN16 uint8_t IV[IBYTES]={0x00,0x00,0x00,0x00,0x00,0x00,
                              0x00,0x00,0x00,0x00,0x00,0x00};
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={};
    ALIGN16 uint8_t EXPECTED_T[16]={0x58,0xe2,0xfc,0xce,0xfa,0x7e,0x30,0x61,
                                  0x36,0x7f,0x1d,0x57,0xa4,0xe7,0x45,0x5a};
    ALIGN16 uint8_t A[MBYTES]={};
#endif

#ifdef TEST2
#define NBYTES 16
#define MBYTES 0
#define IBYTES 12
    ALIGN16 uint8_t K[16]={0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00,
                        0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00};
    ALIGN16 uint8_t P[NBYTES]={0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00,
                             0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00};
    ALIGN16 uint8_t IV[IBYTES]={0x00,0x00,0x00,0x00,0x00,0x00,0x00,0x00,
                              0x00,0x00,0x00,0x00};
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={0x03,0x88,0xda,0xce,0x60,0xb6,0xa3,0x92,
                                      0xf3,0x28,0xc2,0xb9,0x71,0xb2,0xfe,0x78};
    ALIGN16 uint8_t EXPECTED_T[16]={0xab,0x6e,0x47,0xd4,0x2c,0xec,0x13,0xbd,
                                  0xf5,0x3a,0x67,0xb2,0x12,0x57,0xbd,0xdf};
    ALIGN16 uint8_t A[MBYTES]={};
#endif

#ifdef TEST3
#define NBYTES 64
#define MBYTES 0
#define IBYTES 12
    ALIGN16 uint8_t K[16]={0xfe,0xff,0xe9,0x92,0x86,0x65,0x73,0x1c,
                         0x6d,0x6a,0x8f,0x94,0x67,0x30,0x83,0x08};
    ALIGN16 uint8_t P[NBYTES]={0xd9,0x31,0x32,0x25,0xf8,0x84,0x06,0xe5,
                             0xa5,0x59,0x09,0xc5,0xaf,0xf5,0x26,0x9a,
                             0x86,0xa7,0xa9,0x53,0x15,0x34,0xf7,0xda,
                             0x2e,0x4c,0x30,0x3d,0x8a,0x31,0x8a,0x72,
                             0x1c,0x3c,0x0c,0x95,0x95,0x68,0x09,0x53,
                             0x2f,0xcf,0x0e,0x24,0x49,0xa6,0xb5,0x25,
                             0xb1,0x6a,0xed,0xf5,0xaa,0x0d,0xe6,0x57,
                             0xba,0x63,0x7b,0x39,0x1a,0xaf,0xd2,0x55};
    ALIGN16 uint8_t IV[IBYTES]={0xca,0xfe,0xba,0xbe,0xfa,0xce,0xdb,0xad,
                              0xde,0xca,0xf8,0x88};
```

```
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={0x42,0x83,0x1e,0xc2,0x21,0x77,0x74,0x24,
                                        0x4b,0x72,0x21,0xb7,0x84,0xd0,0xd4,0x9c,
                                        0xe3,0xaa,0x21,0x2f,0x2c,0x02,0xa4,0xe0,
                                        0x35,0xc1,0x7e,0x23,0x29,0xac,0xa1,0x2e,
                                        0x21,0xd5,0x14,0xb2,0x54,0x66,0x93,0x1c,
                                        0x7d,0x8f,0x6a,0x5a,0xac,0x84,0xaa,0x05,
                                        0x1b,0xa3,0x0b,0x39,0x6a,0x0a,0xac,0x97,
                                        0x3d,0x58,0xe0,0x91,0x47,0x3f,0x59,0x85};
    ALIGN16 uint8_t EXPECTED_T[16]={0x4d,0x5c,0x2a,0xf3,0x27,0xcd,0x64,0xa6,
                                    0x2c,0xf3,0x5a,0xbd,0x2b,0xa6,0xfa,0xb4};
    ALIGN16 uint8_t A[MBYTES]={};
#endif

#ifdef TEST4
#define NBYTES 60
#define MBYTES 20
#define IBYTES 12
    ALIGN16 uint8_t K[16]={0xfe,0xff,0xe9,0x92,0x86,0x65,0x73,0x1c,
                           0x6d,0x6a,0x8f,0x94,0x67,0x30,0x83,0x08};
    ALIGN16 uint8_t P[NBYTES]={0xd9,0x31,0x32,0x25,0xf8,0x84,0x06,0xe5,
                               0xa5,0x59,0x09,0xc5,0xaf,0xf5,0x26,0x9a,
                               0x86,0xa7,0xa9,0x53,0x15,0x34,0xf7,0xda,
                               0x2e,0x4c,0x30,0x3d,0x8a,0x31,0x8a,0x72,
                               0x1c,0x3c,0x0c,0x95,0x95,0x68,0x09,0x53,
                               0x2f,0xcf,0x0e,0x24,0x49,0xa6,0xb5,0x25,
                               0xb1,0x6a,0xed,0xf5,0xaa,0x0d,0xe6,0x57,
                               0xba,0x63,0x7b,0x39};
    ALIGN16 uint8_t IV[IBYTES]={0xca,0xfe,0xba,0xbe,0xfa,0xce,0xdb,0xad,
                                0xde,0xca,0xf8,0x88};
    ALIGN16 uint8_t A[MBYTES]={0xfe,0xed,0xfa,0xce,0xde,0xad,0xbe,0xef,
                               0xfe,0xed,0xfa,0xce,0xde,0xad,0xbe,0xef,
                               0xab,0xad,0xda,0xd2};
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={0x42,0x83,0x1e,0xc2,0x21,0x77,0x74,0x24,
                                        0x4b,0x72,0x21,0xb7,0x84,0xd0,0xd4,0x9c,
                                        0xe3,0xaa,0x21,0x2f,0x2c,0x02,0xa4,0xe0,
                                        0x35,0xc1,0x7e,0x23,0x29,0xac,0xa1,0x2e,
                                        0x21,0xd5,0x14,0xb2,0x54,0x66,0x93,0x1c,
                                        0x7d,0x8f,0x6a,0x5a,0xac,0x84,0xaa,0x05,
                                        0x1b,0xa3,0x0b,0x39,0x6a,0x0a,0xac,0x97,
                                        0x3d,0x58,0xe0,0x91};
    ALIGN16 uint8_t EXPECTED_T[16]={0x5b,0xc9,0x4f,0xbc,0x32,0x21,0xa5,0xdb,
                                    0x94,0xfa,0xe9,0x5a,0xe7,0x12,0x1a,0x47};
#endif

#ifdef TEST5
#define NBYTES 60
#define MBYTES 20
#define IBYTES 8
    ALIGN16 uint8_t K[16]={0xfe,0xff,0xe9,0x92,0x86,0x65,0x73,0x1c,
                           0x6d,0x6a,0x8f,0x94,0x67,0x30,0x83,0x08};
    ALIGN16 uint8_t P[NBYTES]={0xd9,0x31,0x32,0x25,0xf8,0x84,0x06,0xe5,
                               0xa5,0x59,0x09,0xc5,0xaf,0xf5,0x26,0x9a,
                               0x86,0xa7,0xa9,0x53,0x15,0x34,0xf7,0xda,
                               0x2e,0x4c,0x30,0x3d,0x8a,0x31,0x8a,0x72,
                               0x1c,0x3c,0x0c,0x95,0x95,0x68,0x09,0x53,
                               0x2f,0xcf,0x0e,0x24,0x49,0xa6,0xb5,0x25,
                               0xb1,0x6a,0xed,0xf5,0xaa,0x0d,0xe6,0x57,
                               0xba,0x63,0x7b,0x39};
    ALIGN16 uint8_t A[MBYTES]={0xfe,0xed,0xfa,0xce,0xde,0xad,0xbe,0xef,
```

```
                                0xfe,0xed,0xfa,0xce,0xde,0xad,0xbe,0xef,
                                0xab,0xad,0xda,0xd2};
    ALIGN16 uint8_t IV[IBYTES]={0xca,0xfe,0xba,0xbe,0xfa,0xce,0xdb,0xad};
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={0x61,0x35,0x3b,0x4c,0x28,0x06,0x93,0x4a,
                                         0x77,0x7f,0xf5,0x1f,0xa2,0x2a,0x47,0x55,
                                         0x69,0x9b,0x2a,0x71,0x4f,0xcd,0xc6,0xf8,
                                         0x37,0x66,0xe5,0xf9,0x7b,0x6c,0x74,0x23,
                                         0x73,0x80,0x69,0x00,0xe4,0x9f,0x24,0xb2,
                                         0x2b,0x09,0x75,0x44,0xd4,0x89,0x6b,0x42,
                                         0x49,0x89,0xb5,0xe1,0xeb,0xac,0x0f,0x07,
                                         0xc2,0x3f,0x45,0x98};
    ALIGN16 uint8_t EXPECTED_T[16]={0x36,0x12,0xd2,0xe7,0x9e,0x3b,0x07,0x85,
                                     0x56,0x1b,0xe1,0x4a,0xac,0xa2,0xfc,0xcb};
#endif

#ifdef TEST6
#define NBYTES 60
#define MBYTES 20
#define IBYTES 60
    ALIGN16 uint8_t K[16]={0xfe,0xff,0xe9,0x92,0x86,0x65,0x73,0x1c,
                            0x6d,0x6a,0x8f,0x94,0x67,0x30,0x83,0x08};
    ALIGN16 uint8_t P[NBYTES]={0xd9,0x31,0x32,0x25,0xf8,0x84,0x06,0xe5,
                                0xa5,0x59,0x09,0xc5,0xaf,0xf5,0x26,0x9a,
                                0x86,0xa7,0xa9,0x53,0x15,0x34,0xf7,0xda,
                                0x2e,0x4c,0x30,0x3d,0x8a,0x31,0x8a,0x72,
                                0x1c,0x3c,0x0c,0x95,0x95,0x68,0x09,0x53,
                                0x2f,0xcf,0x0e,0x24,0x49,0xa6,0xb5,0x25,
                                0xb1,0x6a,0xed,0xf5,0xaa,0x0d,0xe6,0x57,
                                0xba,0x63,0x7b,0x39};
    ALIGN16 uint8_t A[MBYTES]={0xfe,0xed,0xfa,0xce,0xde,0xad,0xbe,0xef,
                                0xfe,0xed,0xfa,0xce,0xde,0xad,0xbe,0xef,
                                0xab,0xad,0xda,0xd2};
    ALIGN16 uint8_t IV[IBYTES]={0x93,0x13,0x22,0x5d,0xf8,0x84,0x06,0xe5,
                                 0x55,0x90,0x9c,0x5a,0xff,0x52,0x69,0xaa,
                                 0x6a,0x7a,0x95,0x38,0x53,0x4f,0x7d,0xa1,
                                 0xe4,0xc3,0x03,0xd2,0xa3,0x18,0xa7,0x28,
                                 0xc3,0xc0,0xc9,0x51,0x56,0x80,0x95,0x39,
                                 0xfc,0xf0,0xe2,0x42,0x9a,0x6b,0x52,0x54,
                                 0x16,0xae,0xdb,0xf5,0xa0,0xde,0x6a,0x57,
                                 0xa6,0x37,0xb3,0x9b};
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={0x8c,0xe2,0x49,0x98,0x62,0x56,0x15,0xb6,
                                         0x03,0xa0,0x33,0xac,0xa1,0x3f,0xb8,0x94,
                                         0xbe,0x91,0x12,0xa5,0xc3,0xa2,0x11,0xa8,
                                         0xba,0x26,0x2a,0x3c,0xca,0x7e,0x2c,0xa7,
                                         0x01,0xe4,0xa9,0xa4,0xfb,0xa4,0x3c,0x90,
                                         0xcc,0xdc,0xb2,0x81,0xd4,0x8c,0x7c,0x6f,
                                         0xd6,0x28,0x75,0xd2,0xac,0xa4,0x17,0x03,
                                         0x4c,0x34,0xae,0xe5};
    ALIGN16 uint8_t EXPECTED_T[16]={0x61,0x9c,0xc5,0xae,0xff,0xfe,0x0b,0xfa,
                                     0x46,0x2a,0xf4,0x3c,0x16,0x99,0xd0,0x50};
#endif

#ifdef CUSTOM_TEST
#ifndef NBLOCKS
#define NBLOCKS 64
#endif
#define NBYTES NBLOCKS*16
#define MBYTES 0
#define IBYTES 12
```

```
    ALIGN16 uint8_t K[16]={0xfe,0xff,0xe9,0x92,0x86,0x65,0x73,0x1c,
                         0x6d,0x6a,0x8f,0x94,0x67,0x30,0x83,0x08};
    ALIGN16 uint8_t P[NBYTES]={0xd9,0x31,0x32,0x25,0xf8,0x84,0x06,0xe5,
                             0xa5,0x59,0x09,0xc5,0xaf,0xf5,0x26,0x9a,
                             0x86,0xa7,0xa9,0x53,0x15,0x34,0xf7,0xda,
                             0x2e,0x4c,0x30,0x3d,0x8a,0x31,0x8a,0x72,
                             0x1c,0x3c,0x0c,0x95,0x95,0x68,0x09,0x53,
                             0x2f,0xcf,0x0e,0x24,0x49,0xa6,0xb5,0x25,
                             0xb1,0x6a,0xed,0xf5,0xaa,0x0d,0xe6,0x57,
                             0xba,0x63,0x7b,0x39};
    ALIGN16 uint8_t A[MBYTES]={};
    ALIGN16 uint8_t
IV[IBYTES]={0x93,0x13,0x22,0x5d,0xf8,0x84,0x06,0xe5,0x55,0x90,0x9c,0x5a};
    ALIGN16 uint8_t EXPECTED_C[NBYTES]={0};
    ALIGN16 uint8_t EXPECTED_T[16]={0};
#endif
    ALIGN16 uint8_t C[NBYTES],DECRYPTED_TEXT[NBYTES];
    __m128i T;
    int i,j,tag_correct=1,cipher_correct=1,decrypt_correct=1,decrypt_success;

     /* Verify AES support */
    if (Check_CPU_support_AES( ) == 0) {
        printf ("CPU does not support AES instructions. Bailing out. \n");
        exit (1);
    }
    else printf("CPU check passed. AES instructions are supported.\n\n");

    AES_KEY key;
    AES_128_Key_Expansion (K, key.KEY);
    key.nr = 10;

    AES_GCM_encrypt(P, C, A, IV, &T, NBYTES, MBYTES, IBYTES, key.KEY, key.nr);

    decrypt_success = AES_GCM_decrypt(C, DECRYPTED_TEXT, A, IV, &T, NBYTES, MBYTES,
IBYTES, key.KEY, key.nr);
/*****************************************************************************
Here we print the results of the test
*****************************************************************************/
    print_m128i_with_string("The Key:", *(__m128i*)K);
    printf("\n");

    for(i=0;i<IBYTES/16;i++)
        print_m128i_with_string("The IV:", ((__m128i*)IV)[i]);
    if(IBYTES%16)
        print_m128i_with_string_short("The IV:", ((__m128i*)IV)[i], IBYTES%16);
    printf("\n");

    for(i=0;i<MBYTES/16;i++)
        print_m128i_with_string("The header buffer:", ((__m128i*)A)[i]);
    if(MBYTES%16)
        print_m128i_with_string_short("The header buffer:", ((__m128i*)A)[i],
MBYTES%16);
    if(!MBYTES) printf("NONE\n");
    printf("\n");

    for(i=0;i<NBYTES/16;i++)
        print_m128i_with_string("The PLAINTEXT:", ((__m128i*)P)[i]);
    if(NBYTES%16)
```

```
        print_m128i_with_string_short("The PLAINTEXT:", ((__m128i*)P)[i], NBYTES%16);
    if(!NBYTES) printf("NONE\n");
    printf("\n");

    for(i=0;i<NBYTES/16;i++)
        print_m128i_with_string("The CIPHERTEXT:", ((__m128i*)C)[i]);
    if(NBYTES%16)
        print_m128i_with_string_short("The CIPHERTEXT:", ((__m128i*)C)[i], NBYTES%16);
    if(!NBYTES) printf("NONE\n");
    printf("\n");

    print_m128i_with_string("The tag:",T);
    printf("\n");
//Test correctness
    for(i=0;i<16;i++){
        if(((uint8_t*)&T)[i]!=EXPECTED_T[i]){
            tag_correct=0;
            break;
            }
        }
    for(i=0;i<NBYTES;i++){
        if(C[i]!=EXPECTED_C[i]){
            cipher_correct=0;
            break;
            }
        }
    for(i=0;i<NBYTES;i++){
        if(P[i]!=DECRYPTED_TEXT[i]){
            decrypt_correct=0;
            break;
            }
        }
#ifndef CUSTOM_TEST
    if(tag_correct)
        printf("The tag is equal to the expected tag.\n");
    else
        printf("The tag is NOT EQUAL to the expected tag!!!\n");
    if(cipher_correct)
        printf("The cipher text is equal to the expected cipher text.\n");
    else
        printf("The cipher text is NOT EQUAL to the expected cipher text!!!\n");
#endif
    if(decrypt_success)
        printf("Decryption succeeded.\n");
    else
        printf("Decryption FAILED!!!\n");
    if(decrypt_correct)
        printf("The decrypted text is equal to the original plaintext.\n");
    else
        printf("The decrypted text is NOT EQUAL to the original plaintext!!!\n");
    }
```

Figure 15. AES-GCM (Assembly code): Processing Four Blocks in Parallel with Aggregated Every Four Blocks

```
.align    8
INS:
.quad 0x1000000
```

```
.align    16
ONE:
.quad 0x00000000,0x00000001
.align    16
TWO_N_ONE:
.quad 0x00000002,0x00000001
.align    16
TWO_N_TWO:
.quad 0x00000002,0x00000002
.align    16
FOUR:
.quad 0x00000004,0x00000004
.align    16
BSWAP_MASK:
.byte 15,14,13,12,11,10,9,8,7,6,5,4,3,2,1,0
.align    16
NEUTRAL_MASK:
.byte 0,1,2,3,4,5,6,7,8,9,10,11,12,13,14,15
.align    16
BSWAP_EPI_64:
.byte 7,6,5,4,3,2,1,0,15,14,13,12,11,10,9,8
.align    16
LOAD_HIGH_BROADCAST_AND_BSWAP:
.byte 15,14,13,12,11,10,9,8,15,14,13,12,11,10,9,8


.globl AES_GCM_encrypt
AES_GCM_encrypt:
# parameter 1: %rdi         #*input
# parameter 2: %rsi         #*output
# parameter 3: %rdx         #*addt
# parameter 4: %rcx         #*ivec
# parameter 5: %r8          #*tag
# parameter 6: %r9          # nbytes
# parameter 7: 136 + %rsp    # abytes
# parameter 8: 144 + %rsp   # ibytes
# parameter 9: 152 + %rsp   # *key_schedule
# parameter 10:160 + %rsp   # nr

    pushq   %r10
    pushq   %r11
    pushq   %r12
    pushq   %r13
    pushq   %r14
    pushq   %r15
    pushq   %rax
    pushq   %rbx
    sub     $64, %rsp

HANDLE_IVEC:
    movq    144(%rsp), %rax
    cmp     $12, %rax
    jne     PROCESS_NON96BIT_IVEC
    jmp     PROCESS_96BIT_IVEC

CALCULATE_POWERS_OF_H:
    movdqu  (%rsp), %xmm1
    movdqa  %xmm1, %xmm2
    call    GFMUL
```

```
    movdqu  %xmm1, 16(%rsp)             # 16+rsp holds H^2
    call    GFMUL
    movdqu  %xmm1, 32(%rsp)                # 32+rsp holds H^3
    call    GFMUL
    movdqu  %xmm1, 48(%rsp)                # 48+rsp holds H^4

HANDLE_ADDT:
    pxor    %xmm1, %xmm1
    movq    136(%rsp), %r10             # abytes
    movq    %r10, %r11
    movq    %r10, %r12

    shl     $60, %r12
    shl     $58, %r11
    shr     $6, %r10
    je      ADDT_SINGLES

ADDT_QUADS:                             #hash 4 blocks of header at a time
    movdqu  (%rdx), %xmm10
    movdqu  16(%rdx), %xmm11
    movdqu  32(%rdx), %xmm12
    movdqu  48(%rdx), %xmm13

    add     $64, %rdx
    dec     %r10

    pshufb (BSWAP_MASK), %xmm10
    pshufb (BSWAP_MASK), %xmm11
    pshufb (BSWAP_MASK), %xmm12
    pshufb (BSWAP_MASK), %xmm13

    pxor    %xmm1, %xmm10
    call    REDUCE_FOUR
    jne     ADDT_QUADS

ADDT_SINGLES:                           #hash remaining block
    shrq    $62, %r11
    je      ADDT_REMAINDER
    movdqu  (%rsp), %xmm2
ADDT_SINGLES_LOOP:
    movdqu  (%rdx), %xmm10
    add     $16, %rdx
    dec     %r11
    pshufb  (BSWAP_MASK), %xmm10
    pxor    %xmm10, %xmm1
    call    GFMUL
    jne     ADDT_SINGLES_LOOP

ADDT_REMAINDER:                         #hash the tail (partial block)
    shrq    $60, %r12
    je      HANDLE_DATA
    movq    (%rdx), %rax
    movq    8(%rdx), %rbx
    cmp     $8, %r12
    jl      ADDT_LESS_THEN_8
    jg      ADDT_MORE_THEN_8
    xorq    %rbx, %rbx
    jmp     ADDT_REMAINDER_END
```

```
ADDT_LESS_THEN_8:
    movq    $8, %rcx
    subq    %r12, %rcx
    shlq    $3, %rcx
    shlq    %cl, %rax
    shrq    %cl, %rax
    xorq    %rbx, %rbx
    jmp     ADDT_REMAINDER_END
ADDT_MORE_THEN_8:
    movq    $16, %rcx
    subq    %r12, %rcx
    shlq    $3, %rcx
    shlq    %cl, %rbx
    shrq    %cl, %rbx
ADDT_REMAINDER_END:
    pinsrq  $0, %rax, %xmm3
    pinsrq  $1, %rbx, %xmm3
    pshufb  (BSWAP_MASK), %xmm3
    pxor    %xmm3, %xmm1
    call    GFMUL

HANDLE_DATA:
    movq    %r9, %r10
    movq    %r9, %r11
    movq    %r9, %r12

CALCULATE_COUNTERS:
    movdqa  %xmm0, %xmm15
    pshufb  (LOAD_HIGH_BROADCAST_AND_BSWAP), %xmm15
    paddq   (TWO_N_ONE), %xmm15
    movdqa  %xmm15, %xmm14
    paddq   (TWO_N_TWO), %xmm15
    pshufb  (BSWAP_EPI_64), %xmm14
    pshufb  (BSWAP_EPI_64), %xmm15

    movq    152(%rsp), %rax
    movq    160(%rsp), %rbx

    shl     $60, %r12
    shl     $58, %r11
    shr     $6, %r10
    je      DATA_SINGLES

DATA_QUADS:
    movq    152(%rsp), %r15
    movq    160(%rsp), %r14

    movdqa  %xmm0, %xmm10
    movdqa  %xmm0, %xmm11
    movdqa  %xmm0, %xmm12
    movdqa  %xmm0, %xmm13

    shufpd  $2, %xmm14, %xmm10
    shufpd  $0, %xmm14, %xmm11
    shufpd  $2, %xmm15, %xmm12
    shufpd  $0, %xmm15, %xmm13

    pshufb  (BSWAP_EPI_64), %xmm14
```

```
    pshufb   (BSWAP_EPI_64), %xmm15

    paddq    (FOUR), %xmm14
    paddq    (FOUR), %xmm15

    pshufb   (BSWAP_EPI_64), %xmm14
    pshufb   (BSWAP_EPI_64), %xmm15

    pxor     (%r15), %xmm10
    pxor     (%r15), %xmm11
    pxor     (%r15), %xmm12
    pxor     (%r15), %xmm13

MESSAGE_ENC:
    cmpq     $11, %r14
    movdqa   160(%r15), %xmm9
    aesenc   16(%r15), %xmm10
    aesenc   16(%r15), %xmm11
    aesenc   16(%r15), %xmm12
    aesenc   16(%r15), %xmm13
    aesenc   32(%r15), %xmm10
    aesenc   32(%r15), %xmm11
    aesenc   32(%r15), %xmm12
    aesenc   32(%r15), %xmm13
    aesenc   48(%r15), %xmm10
    aesenc   48(%r15), %xmm11
    aesenc   48(%r15), %xmm12
    aesenc   48(%r15), %xmm13
    aesenc   64(%r15), %xmm10
    aesenc   64(%r15), %xmm11
    aesenc   64(%r15), %xmm12
    aesenc   64(%r15), %xmm13
    aesenc   80(%r15), %xmm10
    aesenc   80(%r15), %xmm11
    aesenc   80(%r15), %xmm12
    aesenc   80(%r15), %xmm13
    aesenc   96(%r15), %xmm10
    aesenc   96(%r15), %xmm11
    aesenc   96(%r15), %xmm12
    aesenc   96(%r15), %xmm13
    aesenc   112(%r15), %xmm10
    aesenc   112(%r15), %xmm11
    aesenc   112(%r15), %xmm12
    aesenc   112(%r15), %xmm13
    aesenc   128(%r15), %xmm10
    aesenc   128(%r15), %xmm11
    aesenc   128(%r15), %xmm12
    aesenc   128(%r15), %xmm13
    aesenc   144(%r15), %xmm10
    aesenc   144(%r15), %xmm11
    aesenc   144(%r15), %xmm12
    aesenc   144(%r15), %xmm13
    jb       MESSAGE_ENC_LAST
    cmpq     $13, %r14
    movdqa   192(%r15), %xmm9
    aesenc   160(%r15), %xmm10
    aesenc   160(%r15), %xmm11
    aesenc   160(%r15), %xmm12
    aesenc   160(%r15), %xmm13
```

```
    aesenc  176(%r15), %xmm10
    aesenc  176(%r15), %xmm11
    aesenc  176(%r15), %xmm12
    aesenc  176(%r15), %xmm13
    jb      MESSAGE_ENC_LAST
    movdqa  224(%r15), %xmm9
    aesenc  192(%r15), %xmm10
    aesenc  192(%r15), %xmm11
    aesenc  192(%r15), %xmm12
    aesenc  192(%r15), %xmm13
    aesenc  208(%r15), %xmm10
    aesenc  208(%r15), %xmm11
    aesenc  208(%r15), %xmm12
    aesenc  208(%r15), %xmm13
MESSAGE_ENC_LAST:
    aesenclast  %xmm9, %xmm10
    aesenclast  %xmm9, %xmm11
    aesenclast  %xmm9, %xmm12
    aesenclast  %xmm9, %xmm13

    pxor    (%rdi), %xmm10
    pxor    16(%rdi), %xmm11
    pxor    32(%rdi), %xmm12
    pxor    48(%rdi), %xmm13

    movdqa  %xmm10, (%rsi)
    movdqa  %xmm11, 16(%rsi)
    movdqa  %xmm12, 32(%rsi)
    movdqa  %xmm13, 48(%rsi)

    add     $64, %rsi
    add     $64, %rdi
    dec     %r10

    pshufb (BSWAP_MASK), %xmm10
    pshufb (BSWAP_MASK), %xmm11
    pshufb (BSWAP_MASK), %xmm12
    pshufb (BSWAP_MASK), %xmm13

    pxor    %xmm1, %xmm10
    call    REDUCE_FOUR
    jne     DATA_QUADS

DATA_SINGLES:
    shrq    $62, %r11
    je      DATA_REMAINDER

    shufpd  $2, %xmm14, %xmm0
    pshufb  (BSWAP_EPI_64), %xmm0
LOOP_DR:
    movq    152(%rsp), %r15
    movq    160(%rsp), %r14
    movdqa  %xmm0, %xmm10
    pshufb  (BSWAP_EPI_64), %xmm10

    paddq   (ONE), %xmm0
    pxor    (%r15), %xmm10
LOOP_DR1:
        addq    $16, %r15
```

```
        dec     %r14
        aesenc  (%r15), %xmm10
        jne     LOOP_DR1
    aesenclast  16(%r15), %xmm10
    pxor    (%rdi), %xmm10
    movdqa  %xmm10, (%rsi)
    addq    $16, %rsi
    addq    $16, %rdi
    dec     %r11
    pshufb  (BSWAP_MASK), %xmm10
    pxor    %xmm10, %xmm1
    call    GFMUL

    jne     LOOP_DR

DATA_REMAINDER:
    shrq    $60, %r12
    je      DATA_END

    movq    152(%rsp), %r15
    movq    160(%rsp), %r14
    pshufb  (BSWAP_EPI_64), %xmm0
    pxor    (%r15), %xmm0
LOOP_DR2:
        addq    $16, %r15
        dec     %r14
        aesenc  (%r15), %xmm0
        jne     LOOP_DR2
    aesenclast  16(%r15), %xmm0
    pxor    (%rdi), %xmm0
    movdqa  %xmm0, (%rsi)

    movq    (%rsi), %rax
    movq    8(%rsi), %rbx
    cmp     $8, %r12
    jl      DATA_LESS_THEN_8
    jg      DATA_MORE_THEN_8
    xorq    %rbx, %rbx
    jmp     DATA_REMAINDER_END
DATA_LESS_THEN_8:
    movq    $8, %rcx
    subq    %r12, %rcx
    shlq    $3, %rcx
    shlq    %cl, %rax
    shrq    %cl, %rax
    xorq    %rbx, %rbx
    jmp     DATA_REMAINDER_END
DATA_MORE_THEN_8:
    movq    $16, %rcx
    subq    %r12, %rcx
    shlq    $3, %rcx
    shlq    %cl, %rbx
    shrq    %cl, %rbx
DATA_REMAINDER_END:
    pinsrq  $0, %rax, %xmm3
    pinsrq  $1, %rbx, %xmm3

    pshufb  (BSWAP_MASK), %xmm3
```

```
    pxor    %xmm3, %xmm1
    call    GFMUL
DATA_END:

    movq    136(%rsp), %r10
    shlq    $3, %r9
    shlq    $3, %r10

    pinsrq  $0, %r9, %xmm3
    pinsrq  $1, %r10, %xmm3

    pxor    %xmm3, %xmm1
    movdqu  (%rsp), %xmm2
    movdqu  (%r8), %xmm10
    call    GFMUL
    pshufb  (BSWAP_MASK), %xmm1
    pxor    %xmm1, %xmm10
    movdqu  %xmm10, (%r8)

END:
    add     $64, %rsp
    popq    %rbx
    popq    %rax
    popq    %r15
    popq    %r14
    popq    %r13
    popq    %r12
    popq    %r11
    popq    %r10
    ret
###############################################################################
PROCESS_96BIT_IVEC:
    movdqu  (%rcx), %xmm0               # xmm0 will hold the Y
    pinsrd  $3, (INS), %xmm0

    movq    152(%rsp), %r15             # key schedule
    movq    160(%rsp), %r12             # number of rounds
    dec     %r12
    movq    %r12, 160(%rsp)
    movdqa  %xmm0, %xmm2
    movdqa  (%r15), %xmm1               # in xmm1 zero block is encrypted
    pxor    (%r15), %xmm2               # in xmm2 Y is encrypted

LOOP_PI1:                               #parallelize aes encryption
        addq    $16, %r15
        dec     %r12
        aesenc  (%r15), %xmm1
        aesenc  (%r15), %xmm2
        jne     LOOP_PI1

    aesenclast  16(%r15), %xmm1
    aesenclast  16(%r15), %xmm2

    pshufb  (BSWAP_MASK), %xmm1         # swap bytes
    movdqu  %xmm2, (%r8)                # store T at *tag
    movdqu  %xmm1, (%rsp)               # store H on stack

    jmp     CALCULATE_POWERS_OF_H
###############################################################################
```

```
PROCESS_NON96BIT_IVEC:
    movq    152(%rsp), %r15              # key schedule
    movq    160(%rsp), %r12              # number of rounds
    movq    160(%rsp), %r12              # number of rounds
    dec     %r12
    movq    %r12, 160(%rsp)

    movdqa  (%r15), %xmm2                # in xmm2 zero block is encrypted

LOOP_PNI1:
        addq    $16, %r15
        dec     %r12
        aesenc  (%r15), %xmm2
        jne     LOOP_PNI1

    aesenclast  16(%r15), %xmm2
    pshufb  (BSWAP_MASK), %xmm2          # swap bytes
    movdqu  %xmm2, (%rsp)                # store H on stack
    pxor    %xmm1, %xmm1                 # Y is zero at first

    movq    144(%rsp), %r10              # ibytes
    movq    %r10, %r11
    movq    %r10, %r12
    xorq    %r13, %r13
    shlq    $3, %r12
    shlq    $60, %r11
    shrq    $4, %r10
    je      PNI_REMAINDER

LOOP_PNI2:                               # hash ivec
        movdqu  (%rcx), %xmm3
        add     $16, %rcx
        dec     %r10
        pshufb  (BSWAP_MASK), %xmm3
        pxor    %xmm3, %xmm1
        call    GFMUL
        jne     LOOP_PNI2

PNI_REMAINDER:                           # hash ivec remainder
    shrq    $60, %r11
    je      PNI_END

    movq    (%rcx), %rax
    movq    8(%rcx), %rbx

    cmp     $8, %r11
    jl      PNI_LESS_THEN_8
    jg      PNI_MORE_THEN_8
    xorq    %rbx, %rbx
    jmp     PNI_REMAINDER_END
PNI_LESS_THEN_8:
    movq    $8, %rcx
    subq    %r11, %rcx
    shlq    $3, %rcx
    shlq    %cl, %rax
    shrq    %cl, %rax
    xorq    %rbx, %rbx
    jmp     PNI_REMAINDER_END
```

```
PNI_MORE_THEN_8:
    movq    $16, %rcx
    subq    %r11, %rcx
    shlq    $3, %rcx
    shlq    %cl, %rbx
    shrq    %cl, %rbx
PNI_REMAINDER_END:
    pinsrq  $0, %rax, %xmm3
    pinsrq  $1, %rbx, %xmm3
    pshufb  (BSWAP_MASK), %xmm3
    pxor    %xmm3, %xmm1
    call    GFMUL

PNI_END:
    pinsrq  $0, %r12, %xmm3
    pinsrq  $1, %r13, %xmm3
    pxor    %xmm3, %xmm1
    call    GFMUL
    pshufb  (BSWAP_MASK), %xmm1
    movdqa  %xmm1, %xmm0

    movq    152(%rsp), %r15             # key schedule
    movq    160(%rsp), %r12             # number of rounds
    pxor    (%r15), %xmm1

LOOP_PNI3:
        addq    $16, %r15
        dec     %r12
        aesenc  (%r15), %xmm1
        jne     LOOP_PNI3

    aesenclast  16(%r15), %xmm1
    movdqu  %xmm1, (%r8)                # store T at *tag

    jmp     CALCULATE_POWERS_OF_H
################################################################################
REDUCE_FOUR:
    movdqa    %xmm13, %xmm1
    movdqa    %xmm12, %xmm3
    movdqa    %xmm11, %xmm5
    movdqa    %xmm10, %xmm7
    movdqa    %xmm13, %xmm2
    movdqa    %xmm12, %xmm4
    movdqa    %xmm11, %xmm6
    movdqa    %xmm10, %xmm8

    pclmulqdq    $0x00, 8(%rsp), %xmm1
    pclmulqdq    $0x00, 24(%rsp), %xmm3
    pclmulqdq    $0x00, 40(%rsp), %xmm5
    pclmulqdq    $0x00, 56(%rsp), %xmm7

    pxor    %xmm3, %xmm1
    pxor    %xmm7, %xmm5
    pxor    %xmm5, %xmm1    #holds xor of low products

    pclmulqdq    $0x11, 8(%rsp), %xmm2
    pclmulqdq    $0x11, 24(%rsp), %xmm4
    pclmulqdq    $0x11, 40(%rsp), %xmm6
    pclmulqdq    $0x11, 56(%rsp), %xmm8
```

```
    pxor     %xmm4, %xmm2
    pxor     %xmm8, %xmm6
    pxor     %xmm6, %xmm2    #holds xor of high products

    pshufd    $78, %xmm13, %xmm3
    pshufd    $78, %xmm11, %xmm5
    pshufd    $78, %xmm12, %xmm4
    pshufd    $78, %xmm10, %xmm6

    pxor %xmm13, %xmm3
    pxor %xmm12, %xmm4
    pxor %xmm11, %xmm5
    pxor %xmm10, %xmm6

    movdqu    8(%rsp), %xmm10
    movdqu    24(%rsp), %xmm11
    movdqu    40(%rsp), %xmm12
    movdqu    56(%rsp), %xmm13

    pshufd    $78, %xmm10, %xmm7
    pshufd    $78, %xmm11, %xmm8
    pshufd    $78, %xmm12, %xmm9

    pxor %xmm10, %xmm7
    pxor %xmm11, %xmm8
    pxor %xmm12, %xmm9

    pshufd  $78, %xmm13, %xmm10
    pxor    %xmm13, %xmm10

    pclmulqdq    $0, %xmm3, %xmm7
    pclmulqdq    $0, %xmm4, %xmm8
    pxor         %xmm7, %xmm8
    pclmulqdq    $0, %xmm5, %xmm9
    pclmulqdq    $0, %xmm6, %xmm10
    pxor         %xmm9, %xmm10

    pxor    %xmm1, %xmm8
    pxor    %xmm2, %xmm10
    pxor    %xmm8, %xmm10

    movdqa  %xmm10, %xmm9
    pslldq  $8, %xmm10
    psrldq  $8, %xmm9

    pxor    %xmm10, %xmm1
    pxor    %xmm9, %xmm2

    movdqa  %xmm1, %xmm3
    movdqa  %xmm2, %xmm6

    movdqa  %xmm3, %xmm4
    movdqa  %xmm6, %xmm5
    psrld   $31, %xmm4
    psrld   $31, %xmm5
    pslld   $1, %xmm3
    pslld   $1, %xmm6

    movdqa  %xmm4, %xmm1
    psrldq  $12, %xmm1
```

```
    pslldq  $4, %xmm4
    pslldq  $4, %xmm5

    por     %xmm4, %xmm3
    por     %xmm5, %xmm6
    por     %xmm1, %xmm6

    movdqa  %xmm3, %xmm4
    movdqa  %xmm3, %xmm5
    movdqa  %xmm3, %xmm1

    pslld   $31, %xmm4
    pslld   $30, %xmm5
    pslld   $25, %xmm1

    pxor    %xmm5, %xmm4
    pxor    %xmm1, %xmm4

    movdqa  %xmm4, %xmm5
    psrldq  $4, %xmm5
    pslldq  $12, %xmm4
    pxor    %xmm4, %xmm3

    pxor    %xmm3, %xmm6
    movdqa  %xmm3, %xmm1
    movdqa  %xmm3, %xmm4
    psrld   $1, %xmm1
    psrld   $2, %xmm4
    psrld   $7, %xmm3
    pxor    %xmm6, %xmm1
    pxor    %xmm4, %xmm1
    pxor    %xmm3, %xmm1
    pxor    %xmm5, %xmm1

    ret
################################################################################
# a = xmm1
# b = xmm2 - remains unchanged
# res = xmm1
# uses also xmm3,xmm4,xmm5,xmm6
GFMUL:
    movdqa    %xmm1, %xmm3
    movdqa    %xmm1, %xmm6
    pclmulqdq $0x00, %xmm2, %xmm3
    pclmulqdq $0x11, %xmm2, %xmm6

    pshufd    $78, %xmm1, %xmm4
    pshufd    $78, %xmm2, %xmm5
    pxor      %xmm1, %xmm4
    pxor      %xmm2, %xmm5
    ##
    pclmulqdq $0x00, %xmm5, %xmm4
    pxor      %xmm3, %xmm4
    pxor      %xmm6, %xmm4

    movdqa    %xmm4, %xmm5
    pslldq    $8, %xmm5
    psrldq    $8, %xmm4

    pxor      %xmm5, %xmm3
```

```
    pxor       %xmm4, %xmm6

    movdqa     %xmm3, %xmm4
    movdqa     %xmm6, %xmm5
    psrld      $31, %xmm4
    psrld      $31, %xmm5
    pslld      $1, %xmm3
    pslld      $1, %xmm6

    movdqa     %xmm4, %xmm1
    psrldq     $12, %xmm1
    pslldq     $4, %xmm4
    pslldq     $4, %xmm5

    por        %xmm4, %xmm3
    por        %xmm5, %xmm6
    por        %xmm1, %xmm6

    movdqa     %xmm3, %xmm4
    movdqa     %xmm3, %xmm5
    movdqa     %xmm3, %xmm1

    pslld      $31, %xmm4
    pslld      $30, %xmm5
    pslld      $25, %xmm1

    pxor       %xmm5, %xmm4
    pxor       %xmm1, %xmm4

    movdqa     %xmm4, %xmm5
    psrldq     $4, %xmm5
    pslldq     $12, %xmm4
    pxor       %xmm4, %xmm3

    pxor       %xmm3, %xmm6
    movdqa     %xmm3, %xmm1
    movdqa     %xmm3, %xmm4
    psrld      $1, %xmm1
    psrld      $2, %xmm4
    psrld      $7, %xmm3
    pxor       %xmm6, %xmm1
    pxor       %xmm4, %xmm1
    pxor       %xmm3, %xmm1
    pxor       %xmm5, %xmm1

    ret
###############################################################################
```

Code Outputs

Figure 16. Test Vector 1: Code Output

```
CPU check passed. AES instructions are supported.
```

```
The Key:                                [0x00000000000000000000000000000000]

The IV:                                 [0x000000000000000000000000]

NONE

NONE

NONE

The tag:                                [0x58e2fccefa7e3061367f1d57a4e7455a]

The tag is equal to the expected tag.
The cipher text is equal to the expected cipher text.
Decryption succeeded.
The decrypted text is equal to the original plaintext.
```

Figure 17. Test Vector 2: Code Output

```
CPU check passed. AES instructions are supported.

The Key:                                [0x00000000000000000000000000000000]

The IV:                                 [0x000000000000000000000000]

NONE

The PLAINTEXT:                          [0x00000000000000000000000000000000]

The CIPHERTEXT:                         [0x0388dace60b6a392f328c2b971b2fe78]

The tag:                                [0xab6e47d42cec13bdf53a67b21257bddf]

The tag is equal to the expected tag.
The cipher text is equal to the expected cipher text.
Decryption succeeded.
The decrypted text is equal to the original plaintext.
```

Figure 18. Test Vector 3: Code Output

```
CPU check passed. AES instructions are supported.

The Key:                                [0xfeffe9928665731c6d6a8f9467308308]

The IV:                                 [0xcafebabefacedbaddecaf888]

NONE

The PLAINTEXT:                          [0xd9313225f88406e5a55909c5aff5269a]
The PLAINTEXT:                          [0x86a7a9531534f7da2e4c303d8a318a72]
The PLAINTEXT:                          [0x1c3c0c95956809532fcf0e2449a6b525]
The PLAINTEXT:                          [0xb16aedf5aa0de657ba637b391aafd255]

The CIPHERTEXT:                         [0x42831ec2217774244b7221b784d0d49c]
The CIPHERTEXT:                         [0xe3aa212f2c02a4e035c17e2329aca12e]
The CIPHERTEXT:                         [0x21d514b25466931c7d8f6a5aac84aa05]
The CIPHERTEXT:                         [0x1ba30b396a0aac973d58e091473f5985]

The tag:                                [0x4d5c2af327cd64a62cf35abd2ba6fab4]

The tag is equal to the expected tag.
```

```
The cipher text is equal to the expected cipher text.
Decryption succeeded.
The decrypted text is equal to the original plaintext.
```

Figure 19. Test Vector 4: Code Output

```
CPU check passed. AES instructions are supported.

The Key:                                [0xfeffe9928665731c6d6a8f9467308308]

The IV:                                 [0xcafebabefacedbaddecaf888]

The header buffer:                      [0xfeedfacedeadbeeffeedfacedeadbeef]
The header buffer:                      [0xabaddad2]

The PLAINTEXT:                          [0xd9313225f88406e5a55909c5aff5269a]
The PLAINTEXT:                          [0x86a7a9531534f7da2e4c303d8a318a72]
The PLAINTEXT:                          [0x1c3c0c95956809532fcf0e2449a6b525]
The PLAINTEXT:                          [0xb16aedf5aa0de657ba637b39]

The CIPHERTEXT:                         [0x42831ec2217774244b7221b784d0d49c]
The CIPHERTEXT:                         [0xe3aa212f2c02a4e035c17e2329aca12e]
The CIPHERTEXT:                         [0x21d514b25466931c7d8f6a5aac84aa05]
The CIPHERTEXT:                         [0x1ba30b396a0aac973d58e091]

The tag:                                [0x5bc94fbc3221a5db94fae95ae7121a47]

The tag is equal to the expected tag.
The cipher text is equal to the expected cipher text.
Decryption succeeded.
The decrypted text is equal to the original plaintext.
```

Figure 20. Test Vector 5: Code Output

```
CPU check passed. AES instructions are supported.

The Key:                                [0xfeffe9928665731c6d6a8f9467308308]

The IV:                                 [0xcafebabefacedbad]

The header buffer:                      [0xfeedfacedeadbeeffeedfacedeadbeef]
The header buffer:                      [0xabaddad2]

The PLAINTEXT:                          [0xd9313225f88406e5a55909c5aff5269a]
The PLAINTEXT:                          [0x86a7a9531534f7da2e4c303d8a318a72]
The PLAINTEXT:                          [0x1c3c0c95956809532fcf0e2449a6b525]
The PLAINTEXT:                          [0xb16aedf5aa0de657ba637b39]

The CIPHERTEXT:                         [0x61353b4c2806934a777ff51fa22a4755]
The CIPHERTEXT:                         [0x699b2a714fcdc6f83766e5f97b6c7423]
The CIPHERTEXT:                         [0x73806900e49f24b22b097544d4896b42]
The CIPHERTEXT:                         [0x4989b5e1ebac0f07c23f4598]

The tag:                                [0x3612d2e79e3b0785561be14aaca2fccb]

The tag is equal to the expected tag.
The cipher text is equal to the expected cipher text.
Decryption succeeded.
The decrypted text is equal to the original plaintext.
```

Figure 21. Test Vector 6: Code Output

```
CPU check passed. AES instructions are supported.

The Key:                                [0xfeffe9928665731c6d6a8f9467308308]

The IV:                                 [0x9313225df88406e555909c5aff5269aa]
The IV:                                 [0x6a7a9538534f7da1e4c303d2a318a728]
The IV:                                 [0xc3c0c95156809539fcf0e2429a6b5254]
The IV:                                 [0x16aedbf5a0de6a57a637b39b]

The header buffer:                      [0xfeedfacedeadbeeffeedfacedeadbeef]
The header buffer:                      [0xabaddad2]

The PLAINTEXT:                          [0xd9313225f88406e5a55909c5aff5269a]
The PLAINTEXT:                          [0x86a7a9531534f7da2e4c303d8a318a72]
The PLAINTEXT:                          [0x1c3c0c95956809532fcf0e2449a6b525]
The PLAINTEXT:                          [0xb16aedf5aa0de657ba637b39]

The CIPHERTEXT:                         [0x8ce24998625615b603a033aca13fb894]
The CIPHERTEXT:                         [0xbe9112a5c3a211a8ba262a3cca7e2ca7]
The CIPHERTEXT:                         [0x01e4a9a4fba43c90ccdcb281d48c7c6f]
The CIPHERTEXT:                         [0xd62875d2aca417034c34aee5]

The tag:                                [0x619cc5aefffe0bfa462af43c1699d050]

The tag is equal to the expected tag.
The cipher text is equal to the expected cipher text.
Decryption succeeded.
The decrypted text is equal to the original plaintext.
```

PCLMULQDQ and GFMUL Test Vectors

This chapter provides a few test vectors. "Little Endian" notation is used unless specified otherwise.

PCLMULQDQ Test Vectors

The following first 4 test vectors have the same xmm1 and xmm2 input, and vary only in the value of the immediate byte. This way, the result of all of the four combinations, High/Low from xmm1 and xmm2, are generates. Only bits [4] and [0] of the immediate byte are used for selecting the multiplicands.

```
Input to the PCLMULQDQ instruction
xmm1 = 7b5b54657374566563746f725d53475d
xmm2 = 48692853686179295b477565726f6e5d

The corresponding 64-bit Low/High halves are
xmm1High = 7b5b546573745665   xmm1Low = 63746f725d53475d
xmm2High = 4869285368617929   xmm2Low = 5b477565726f6e5d

Test Vector 1:
immediate = 0x00; carry-less multiply xmm2Low by xmm1Low
PCLMULQDQ result = 1d4d84c85c3440c0929633d5d36f0451
```

```
Test Vector 2:
immediate = 0x10; carry-less multiply xmm2High by xmm1Low
PCLMULQDQ result = 1bd17c8d556ab5a17fa540ac2a281315

Test Vector 3:
immediate = 0x01; carry-less multiply xmm2Low by xmm1High
PCLMULQDQ result = 1a2bf6db3a30862fbabf262df4b7d5c9

Test Vector 4:
immediate = 0x11; carry-less multiply xmm2High by xmm1High
PCLMULQDQ result = 1d1e1f2c592e7c45d66ee03e410fd4ed

Test Vector 5:
xmm1 = 00000000000000008000000000000000
xmm2 = 00000000000000008000000000000000
immediate = 0x00
PCLMULQDQ result = 40000000000000000000000000000000
```

Multiplication in GF(2^{128}) Defined by the Polynomial $x^{128} + x^7 + x^2 + x + 1$

```
a =             0x7b5b54657374566563746f725d53475d
b =             0x48692853686179295b477565726f6e5d
GFMUL128 (a, b) =      0x40229a09a5ed12e7e4e10da323506d2
```

(GFMUL128 (a, b) is the multiplication results of a and b, in GF(2^{128}) defined by the reduction polynomial $g = g(x) = x^{128} + x^7 + x^2 + x + 1$)

GCM Test Vector

The following test vector takes into account the special peculiarity of GCM which specifies that the bits of the input operands (data and hash keys) and the output operand should be reflected

```
Data:                   0x952b2a56a5604ac0b32b6656a05b40b6
Hash Key:               0xdfa6bf4ded81db03ffcaff95f830f061
Multiplication Result:  0xda53eb0ad2c55bb64fc4802cc3feda60
```

Explanation: For a 128 bits quantity X, Reflect (X) is defined as the 128 bits quantity Y whose i-th bit equal to the (127-i)-th bit of X, (for $0 \le 0 \le 127$).

If

```
A = 0x952b2a56a5604ac0b32b6656a05b40b6
B = 0xdfa6bf4ded81db03ffcaff95f830f061
```

And,

```
C = Reflect (A) * Reflect (B)
```

("*" is in GF(2^{128}) defined by the polynomial $g = g(x) = x^{128} + x^7 + x^2 + x + 1$))

Then

```
Reflect (A) = 0x6d02da056a66d4cd035206a56a54d4a9
Reflect (B) = 0x860f0c1fa9ff53ffc0db81b7b2fd65fb
C = 0x65B7FC3340123F26DDAA34B50D7CA5B
```

Finally,

```
Reflect (C) = 0xda53eb0ad2c55bb64fc4802cc3feda60
```

Which is the "Multiplication Result" obtained above.

Performance

This chapter provides the performance numbers of the code examples which were given above, and, for comparison, the performance of code that does not use Intel AES New Instructions / PCLMULQDQ instruction (running on the same platform).

The experiments were carried out on a processor based on Intel microarchitecture codename Westmere running at 2.67 GHz. The system was run with Intel® Turbo Boost Technology, Intel® Hyper-Threading Technology, and Enhanced Intel Speedstep® Technology disabled, and no X server and no network daemon running. The operating system was Linux (OpenSuse 11.1 64 bits).

The C code parts were compiled using icc version 11.0 with the –O3 flag. For the AES-GCM, the key was pre-expanded, and the key expansion overhead was not counted. Table 1, below, provides performance numbers for three buffer sizes.

The performance results are summarized in Table 1. The top part of Table 1 shows several implementations of AES-GCM, using the algorithms which were provided in the paper. The bottom part of Table 1 shows the performance of code that does not use the PCLMULQDQ and the Intel AES New Instructions.

	Code Reference	Comments	Performance in CPU cycles per byte		
			Buffer Size: 1 KB	Buffer Size: 4 KB	Buffer Size: 16 KB
1	Fig. 5 + Fig. 9	AES-CTR parallelizing 4 blocks at a time; ghash operates on one block	5.49	5.36	5.33

		at a time. GFmul implemented using schoolbook and Algorithm 5.			
2	Fig.7 + Fig. 11	AES-CTR parallelizing 4 blocks at a time; ghash operates on one block at a time. GFmul implemented using Karatsuba and Algorithm 4.	5.08	4.94	4.91
3	Fig. 8 + Fig. 12	AES-CTR parallelizing 4 blocks at a time; ghash operates on 4 blocks at a time. GFmul implemented using Schoolbook and Algorithm 5.	4.16	3.88	3.70
4	Fig. 15	ASM AES-CTR parallelizing 4 blocks and Ghashing 4 blocks at a time in assembly	3.85	3.60	3.54
Performance of implementations that do not use PCLMULQDQ and AES instructions					
5	Fig. 2 + Fig.9 (Solaris)	AES-CTR parallelize 4 blocks, ghash one block at a time. GFmul using Solaris function. (*)	188.9	187.69	187.40
6	Gladman	Brian Gladman's GCM, taken from his website, using fastest method of 64K lookup tables (**)	22.69	22.27	21.96

Table 1. The Performance of AES-128 in GCM Mode (on a processor based on Intel microarchitecture codename Westmere)

(*) The code was downloaded from http://src.opensolaris.org/source/xref/onnv/onnv-gate/usr/src/common/crypto/modes/gcm.c#46 (on September, 2009)

(**) The code was downloaded from http://gladman.plushost.co.uk/oldsite/AES/index.php (July 2009)

Discussion

The significant speedup gained from using the PCLMULQDQ instruction and the Intel AES New Instructions, together with the proposed algorithms is evident.

For the cases where the GHASH is computed one block at a time, Table 1 shows that bit-reflecting the input it faster than the shift-by-one method (Algorithm 5). However, the picture changes when the GHASH is aggregated and computed only once per four (or more) blocks at a time. Then, the shift-by-one method allows for processing the input data (the ciphertext from the AES-CTR part of the algorithm) without bit-reflection, and the reduction modulo $x^{128} + x^7 + x^2 + x + 1$ occurs less frequently. In this case, the aggregated reduction method outperforms the other approaches, achieving performance of 3.54 Cycles/Byte (for long buffers). Note that in CTR mode

the counter is encrypted (rather than the data). Therefore, the number of blocks which are processed in parallel, and the number of blocks which are aggregated before computing a reduction, is an implementation preference.

Table 1 also shows that performance improved with longer buffers. This is due to the fact the overhead for the initialization of the H value (s), and for the CTR mode is amortized over a larger chunk of data. For 4K buffer (and longer), the fastest implementation performs is more than 6 times faster than the existing implementations that use lookup tables.

Summary

This paper presented Intel's, new instruction, namely PCLMULQDQ, that performs carry-less multiplication of two 64-bit operands. We provided information on using PCLMULQDQ for computing the Galois Hash portion of the Galois Counter Mode. We also detailed several methods for using PCLMULQDQ and Intel AES New Instructions in order to implement AES-GCM. The reported performance numbers show significant speedup in AES-GCM, compared lookup tables based sowtware implementations.

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